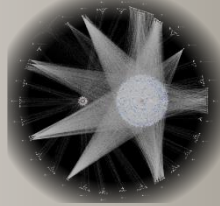


Torino

ECML PKDD 2023

September 18 - 22 2023

Construction and Training of Multi-Associative Graph Networks



[Adrian Horzyk](#)



Daniel Bulanda



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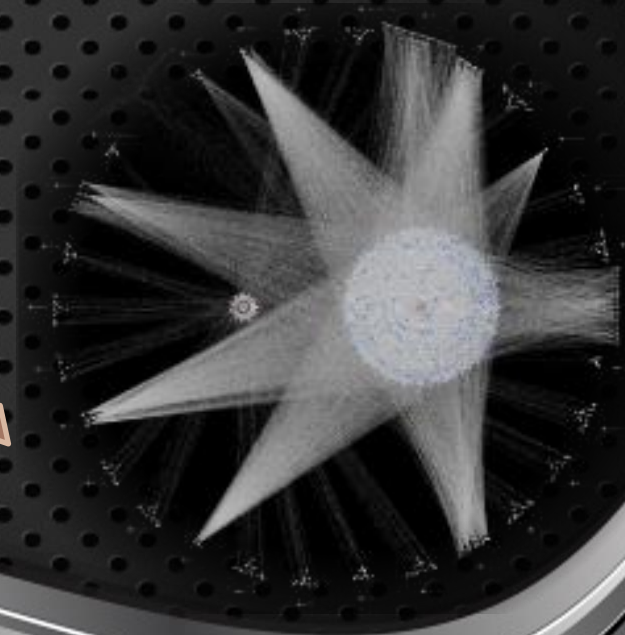


AGH University of Krakow - University of Information Technology and Management in Rzeszow - Ohio University in Athens





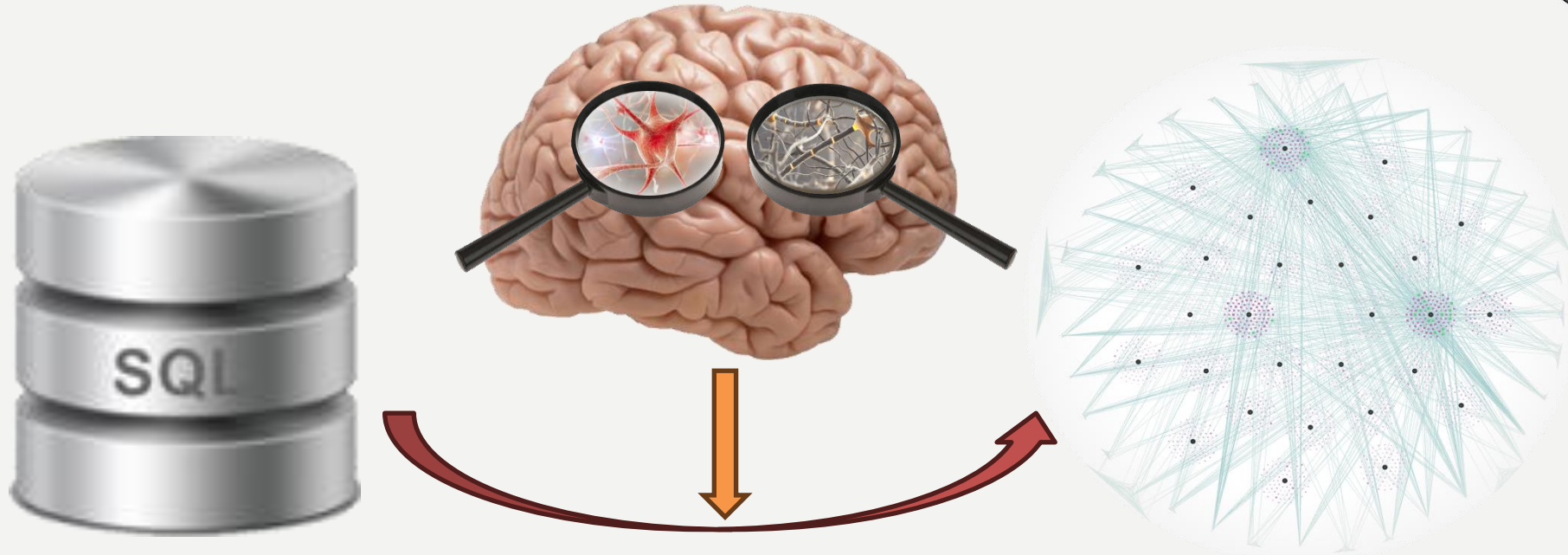
Aim and Objectives



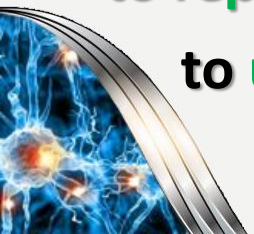
Construction and Training of
Multi-Associative Graph Networks

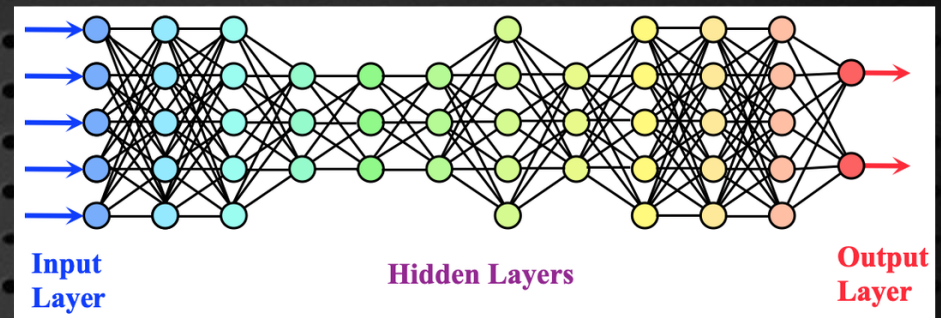


Aim and Objectives



The goal of this research is to understand how **data and relationships** are represented **in the brains** and use this information to represent multiple data of any kind in graph-based structures that behave like neural networks to **represent knowledge** about **the data, objects, and their relations** to **use it for solving different computational intelligence tasks** efficiently without predefined targets before „training“.



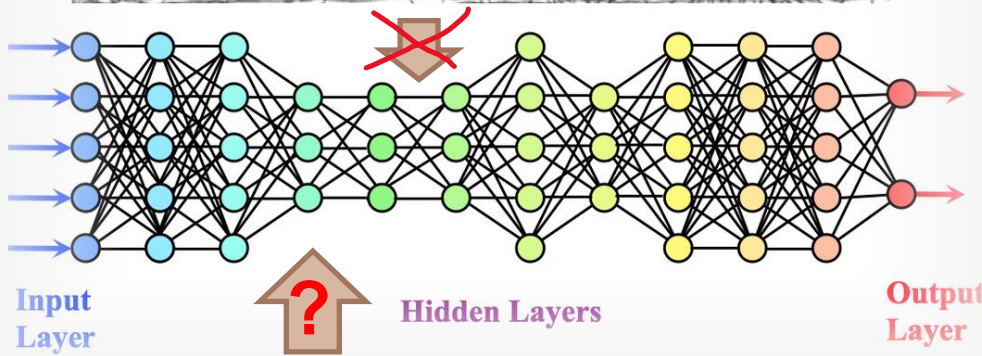
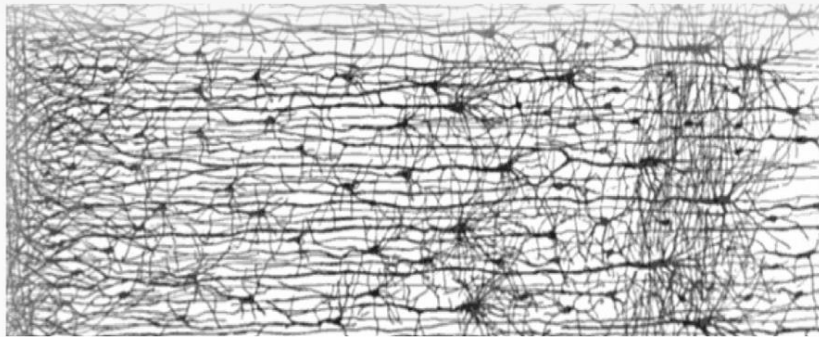
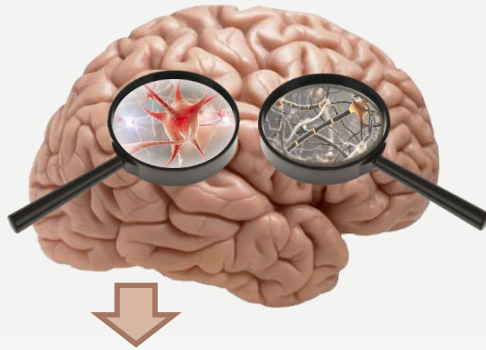


How do brains differ from contemporary neural networks?

Construction and Training of Multi-Associative Graph Networks



Essential Differences



How to use data stored in various databases efficiently in brain-like manner?

Brains contain **sparse, irregular, lateral, recurrent, adaptable, and dynamically developed connections** during the life-long training process, reproducing diverse relationships between represented objects by neurons, while

contemporary NN structures are usually **rigid, regular, layered, and feed-forward** with **predefined inputs and outputs** containing regular **all-to-all** or **many-to-many** area-limited connections that can adapt only weights.





Insufficient DB representation of data relationships

Construction and Training of
Multi-Associative Graph Networks



RDB Relationship Representation

Data stored in RDBs are usually imperfectly normalized and aggregated to avoid too many join operations that impact search efficiency.

table: doctors				
id_doc	first_name	last_name	experience	specialization
D1	John	Smith	25	Surgery
D2	Tom	Allen	10	Radiology
D3	David	Jolie	45	Surgery
D4	John	Smith	8	Oncology
D5	Raul	Willis	2	Patology
D6	Lucy	Hanks	25	Radiology
D7	Nina	Ford	10	Surgery
D8	Tom	Cage	2	Surgery

link table: doctors-patients	
id_doc	id_pat
D2	P4
D7	P4
D2	P6
D7	P6
D2	P7
D4	P7
D6	P7
D7	P7
D5	P7
D5	P1
D5	P2
D1	P3
D3	P3
D8	P5
D7	P5
D1	P8
D8	P8
D3	P9
D7	P9
D2	P2
D2	P5
D6	P8
D6	P9

table: patients					
id_pat	first_name	last_name	age	disease	room_id
P1	John	Cage	35	Lupus	R4
P2	John	Smith	58	Lupus	R1
P3	Emma	Hanks	42	Colitis	R3
P4	Nina	Ford	70	Pneumonia	R4
P5	Lucy	Allen	70	Colitis	R3
P6	Sara	Ford	25	Pneumonia	R4
P7	Cate	Bosch	62	Glioma	R3
P8	David	Smith	42	Infarct	R1
P9	Raul	Willis	25	Infarct	R2

table: nurses			
id_nur	first_name	last_name	experience
N1	Cate	Bosch	25
N2	Emma	Allen	8
N3	Nina	Smith	10
N4	Sara	Ford	2

link table: nurses-rooms	
id_nur	id_rom
N1	R3
N1	R4
N2	R3
N2	R4
N3	R1
N3	R2
N4	R1
N4	R2

table: rooms		
id_rom	type	beds
R1	PostOp	3
R2	Emergency	2
R3	Ward	4
R4	Ward	5

Many relationships require the use of queries to find them.

RDBs represent only a small part of useful relationships, while **similarity, order, and the same values** of attributes of objects stored in the same or different tables **are unrepresented.**





Associative DB Transformation to a Multi-Associative Graph Network

Construction and Training of
Multi-Associative Graph Networks



Associative Transformation Algorithm

Let's transform all **Relational Database (RDB) tables** to the graph structure **aggregating** all the same values in the same nodes, **connecting** all neighbor values in order, **joining** all tables' columns of all RDBs representing the same categories, following the presented algorithm:



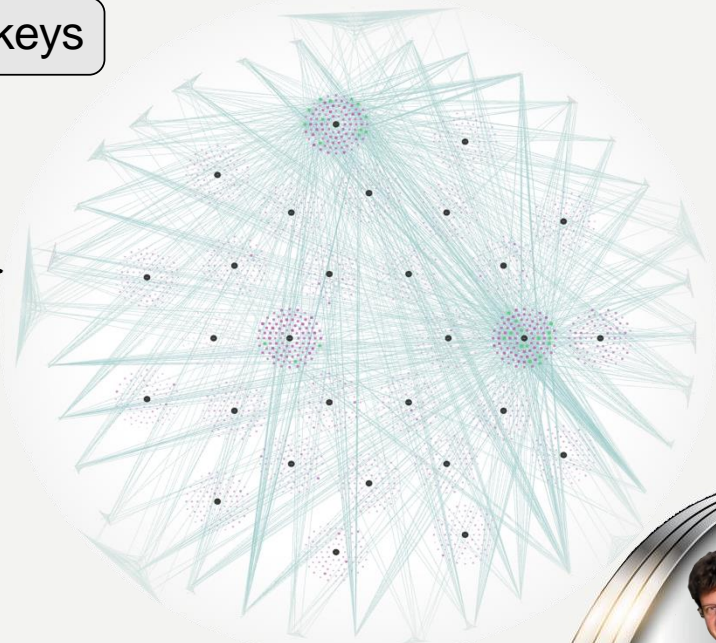
Transform the tables that do not contain any foreign keys

Are
all tables already
transformed?

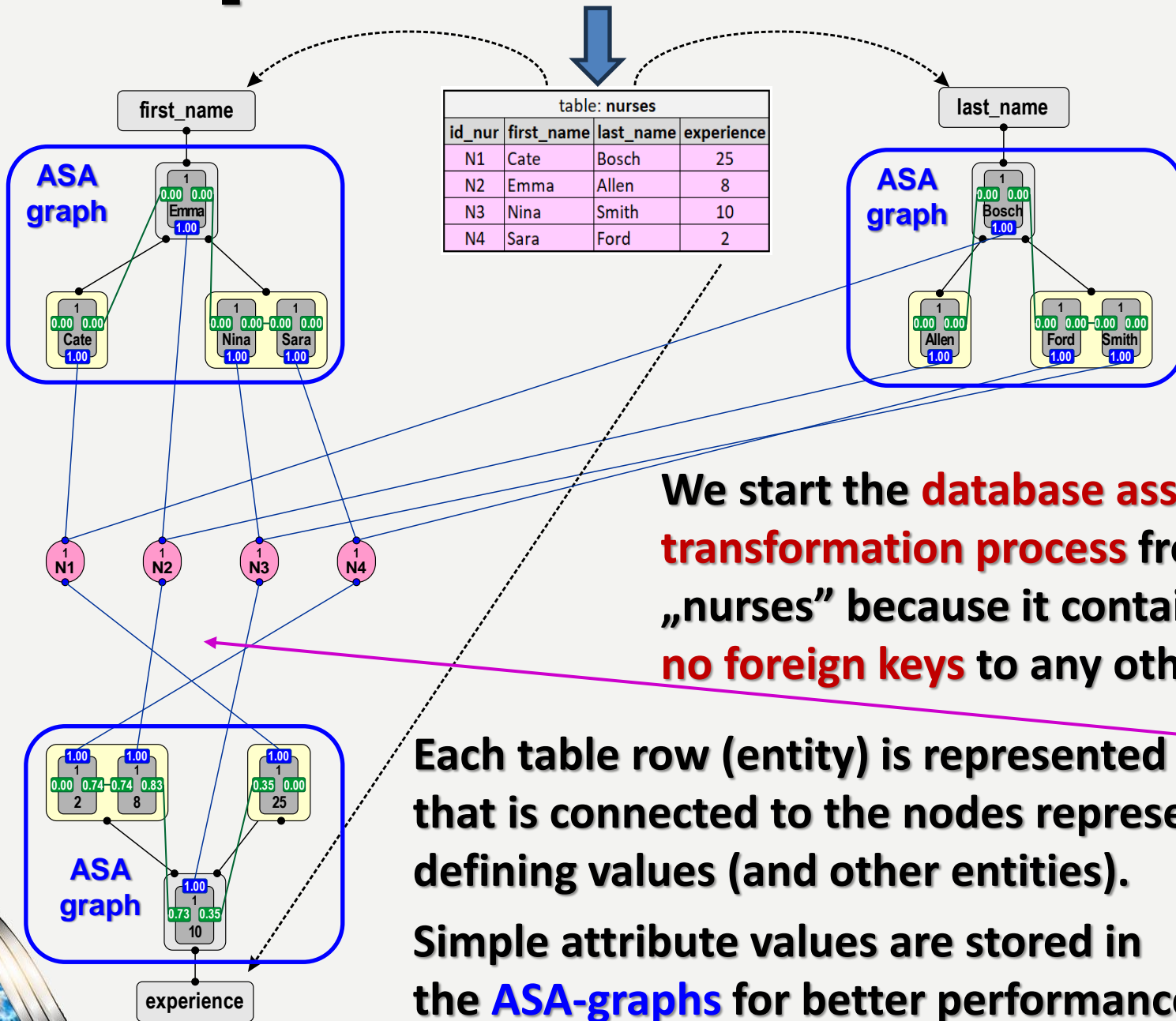
Yes

No

Transform the tables that
contain only foreign keys
to the already transformed tables



Example of Associative Transformation



We start the **database associative transformation process** from table „nurses” because it contains **no foreign keys** to any other tables.

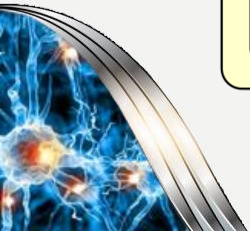
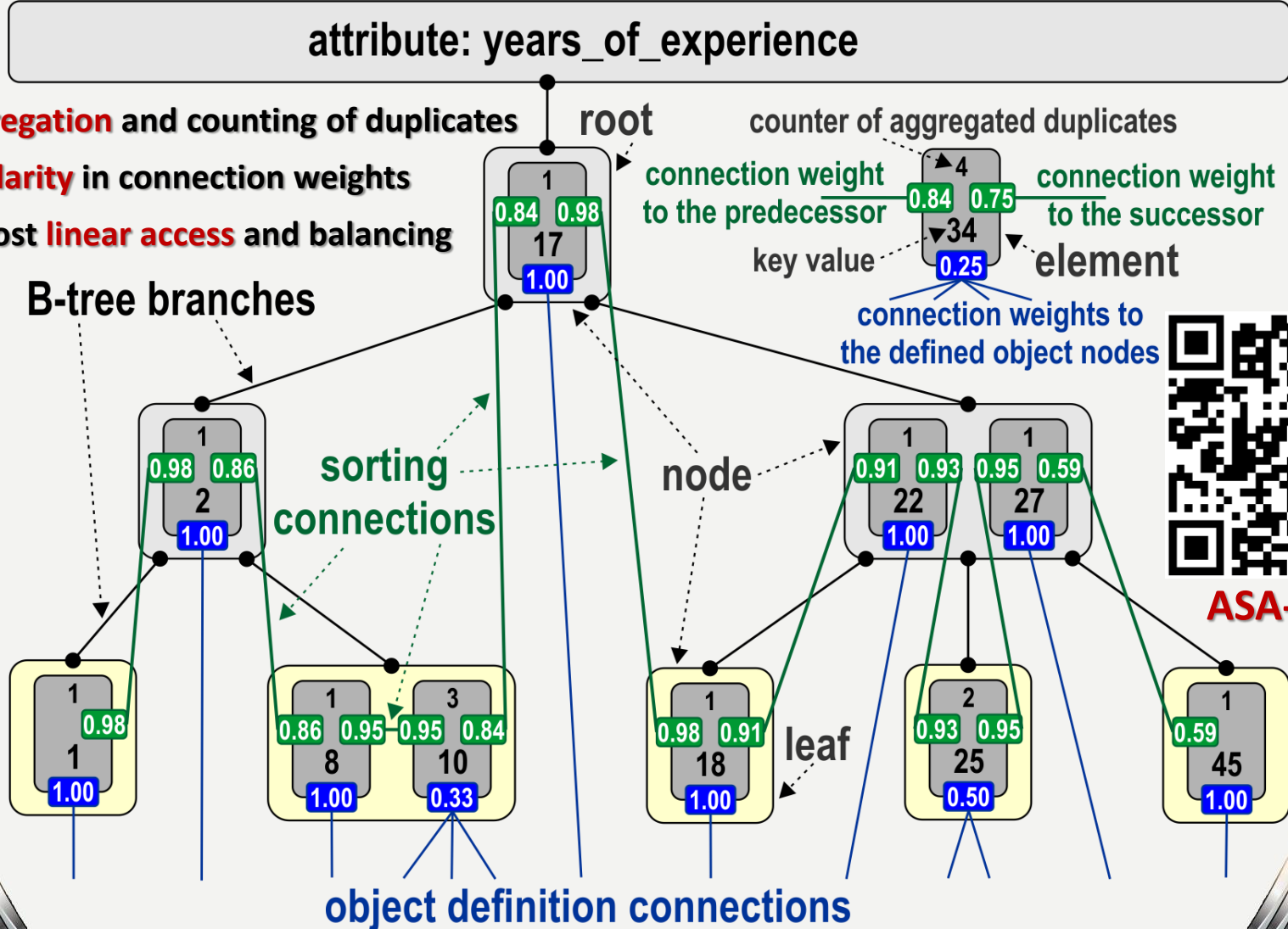
Each table row (entity) is represented by a **node** that is connected to the nodes representing its defining values (and other entities). Simple attribute values are stored in the **ASA-graphs** for better performance.



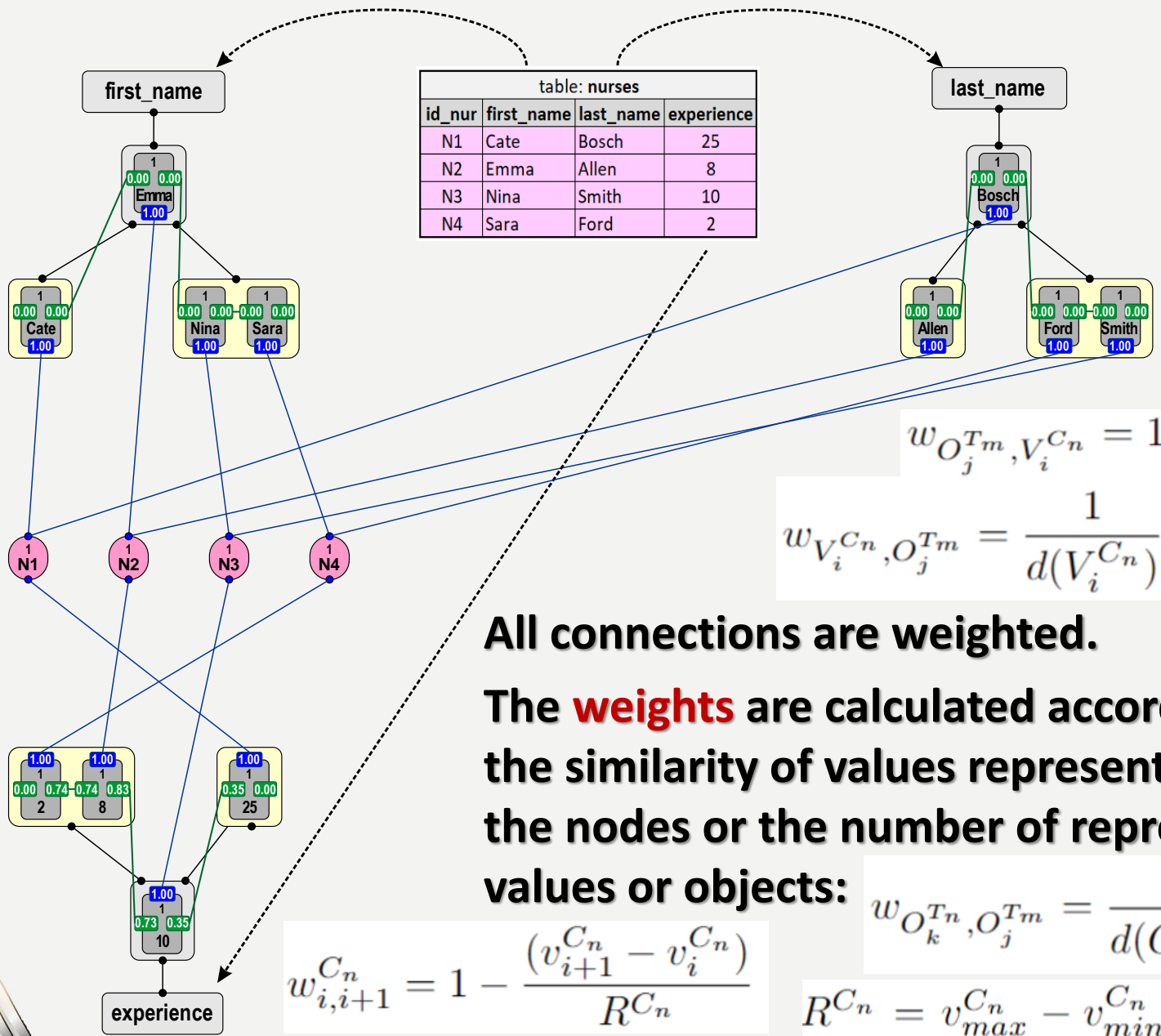
ASA-graph

ASA-graph is an associative self-sorting and self-balancing B-tree-based graph structure for representing attribute values **in the sorted order**:

- **Aggregation** and counting of duplicates
- **Similarity** in connection weights
- Almost **linear access** and balancing



Example of Associative Transformation



$$w_{O_j^{T_m}, V_i^{C_n}} = 1$$

$$w_{V_i^{C_n}, O_j^{T_m}} = \frac{1}{d(V_i^{C_n})}$$

All connections are weighted.

The **weights** are calculated according to the similarity of values represented by the nodes or the number of represented values or objects:

$$w_{i,i+1}^{C_n} = 1 - \frac{(v_{i+1}^{C_n} - v_i^{C_n})}{R^{C_n}}$$

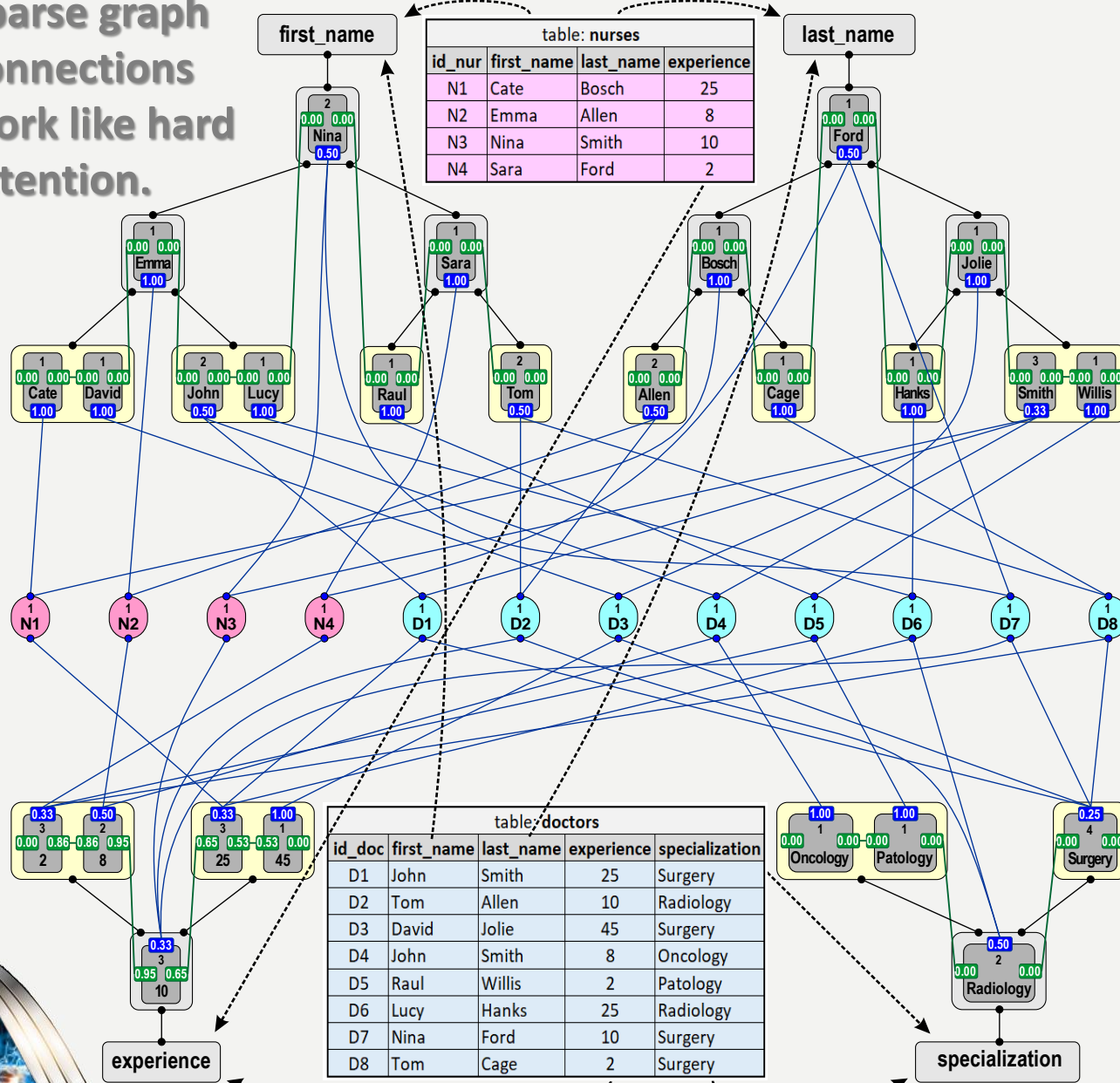
$$w_{O_k^{T_n}, O_j^{T_m}} = \frac{1}{d(O_k^{T_n})}$$

$$R^{C_n} = v_{max}^{C_n} - v_{min}^{C_n}$$



Example of Associative Transformation

Sparse graph connections work like hard attention.

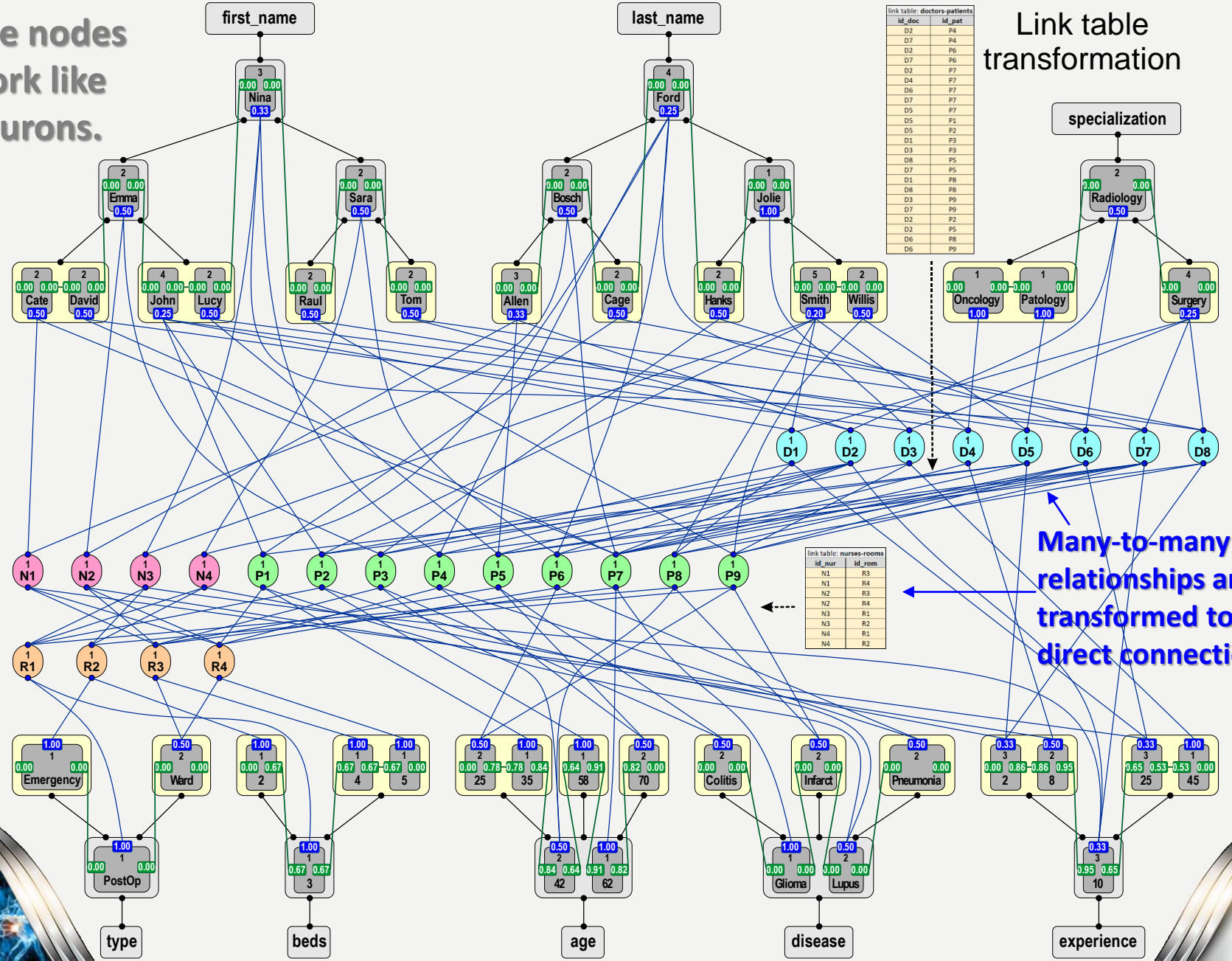


In the next steps, the other tables are transformed and their values are aggregated in the same ASA-graphs if belonging to the same data categories, e.g.: „first_name”, „last_name”, or „experience”, and counters and weights are updated.



Example of Associative Transformation

The nodes work like neurons.



link table: doctors-patients

id_doc	id_pat
D2	P4
D7	P4
D2	P6
D7	P6
D2	P7
D4	P7
D6	P7
D7	P7
D5	P7
D5	P1
D5	P2
D1	P3
D3	P3
D8	P5
D7	P5
D1	P8
D8	P8
D3	P9
D7	P9
D2	P2
D2	P5
D6	P8
D6	P9

Link table transformation

link table: nurses-rooms

id_nur	id_rom
N1	R3
N1	R4
N2	R3
N2	R4
N3	R1
N3	R2
N4	R1
N4	R2

Many-to-many relationships are transformed to direct connections.



MAGN Constructed for RDB

table: patients					
id_pat	first_name	last_name	age	disease	room_id
P1	John	Cage	35	Lupus	4
P2	John	Smith	58	Lupus	1
P3	Emma	Hanks	42	Colitis	3
P4	Nina	Ford	70	Pneumonia	4
P5	Lucy	Allen	70	Colitis	3
P6	Sara	Ford	25	Pneumonia	4
P7	Cate	Bosch	62	Glioma	3
P8	David	Smith	42	Infarct	1
P9	Raul	Willis	25	Infarct	2

table: doctors				
id_doc	first_name	last_name	experience	specialization
D1	John	Smith	25	Surgery
D2	Tom	Allen	10	Radiology
D3	David	Jolie	45	Surgery
D4	John	Smith	8	Oncology
D5	Raul	Willis	2	Patology
D6	Lucy	Hanks	25	Radiology
D7	Nina	Ford	10	Surgery
D8	Tom	Cage	2	Surgery

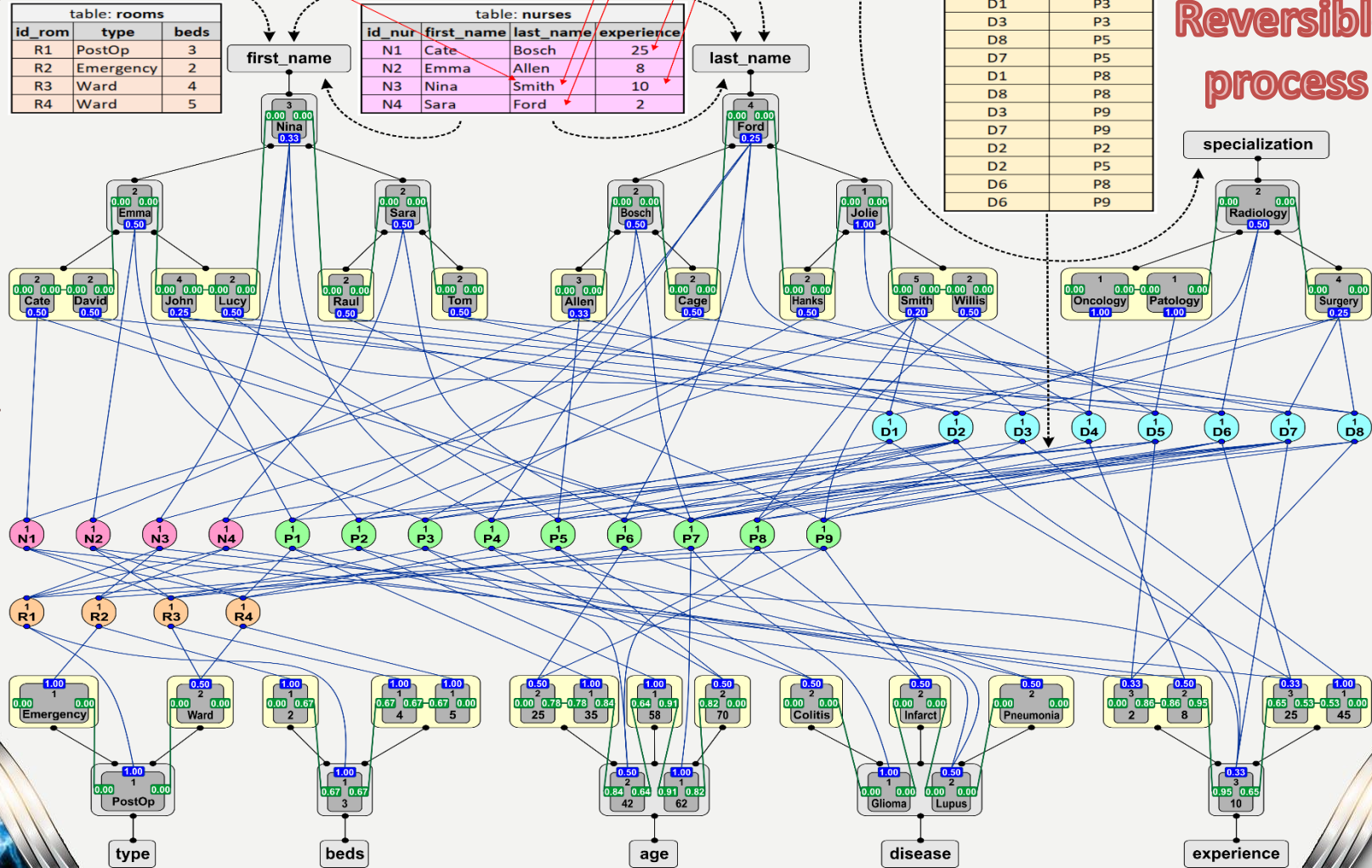
link table: doctors-patients	
id_doc	id_pat
D2	P4
D7	P4
D2	P6
D7	P6
D2	P7
D4	P7
D6	P7
D7	P7
D5	P7
D5	P1
D5	P2
D1	P3
D3	P3
D8	P5
D7	P5
D1	P8
D8	P8
D3	P9
D7	P9
D2	P2
D2	P5
D6	P8
D6	P9

link table: nurses-rooms	
id_nur	id_rom
N1	R3
N1	R4
N2	R3
N2	R4
N3	R1
N3	R2
N4	R1
N4	R2

table: rooms		
id_rom	type	beds
R1	PostOp	3
R2	Emergency	2
R3	Ward	4
R4	Ward	5

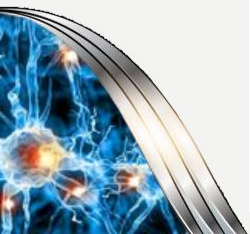
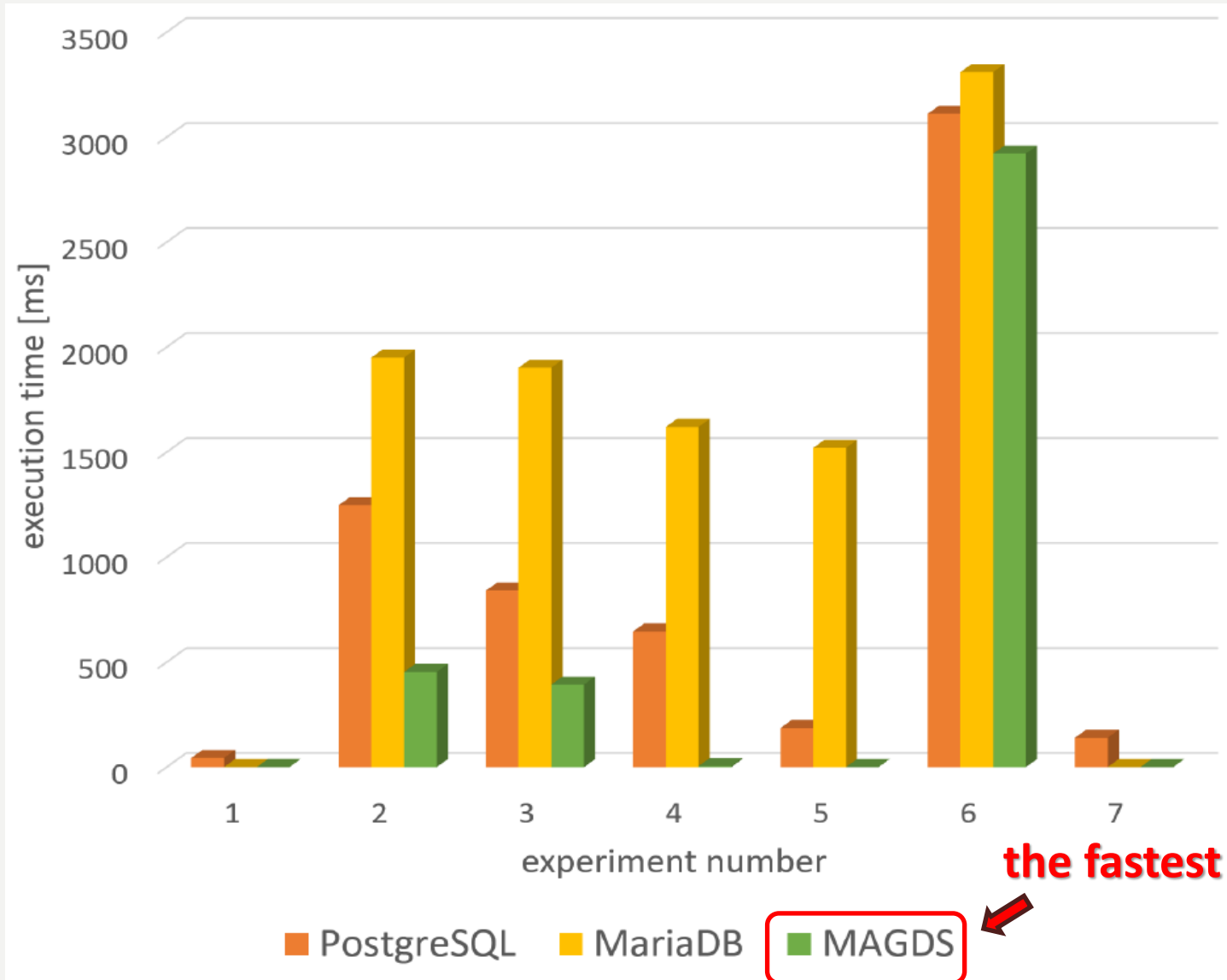
table: nurses				
id_nur	first_name	last_name	experience	specialization
N1	Cate	Bosch	25	
N2	Emma	Allen	8	
N3	Nina	Smith	10	
N4	Sara	Ford	2	

Reversible process



Efficiency of MAGNs

Comparisons of **SQL query times** of **MAGNs** and **RDBMs** in milliseconds:



Queries Used in the Comparisons

Experiment 1

```
select age from gxd_specimen limit 100;
```

Experiment 2

```
select distinct sp.specimenlabel
from gxd_specimen sp
inner join gxd_genotype ge
on sp._genotype_key = ge._genotype_key
inner join prb_strain st
on ge._strain_key = st._strain_key
inner join mgi_user us
on st._createdby_key = us._user_key
where agemin in (select min(agemin) from gxd_specimen)
or agemin in (select max(agemin) from gxd_specimen)
and agemax in (select min(agemax) from gxd_specimen)
or agemax in (select max(agemax) from gxd_specimen)
and ge.isconditional = 0
and st.standard = 1
and st.private = 0
order by specimenlabel;
```

Experiment 3

```
select sum(sp.sequencenum) / count(sp.sequencenum)
from gxd_specimen sp
inner join gxd_genotype ge
on sp._genotype_key = ge._genotype_key
inner join prb_strain st
on ge._strain_key = st._strain_key
inner join mgi_user us
on st._createdby_key = us._user_key
where agemin in (select min(agemin) from gxd_specimen)
or agemin in (select max(agemin) from gxd_specimen)
and agemax in (select min(agemax) from gxd_specimen)
or agemax in (select max(agemax) from gxd_specimen)
and ge.isconditional = 0
and st.standard = 1
and st.private = 0;
```

Experiment 4

```
select count(distinct insertsize) from prb_probe;
```

Experiment 5

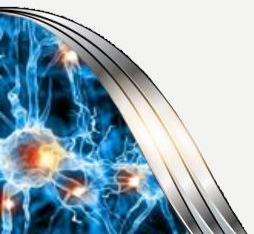
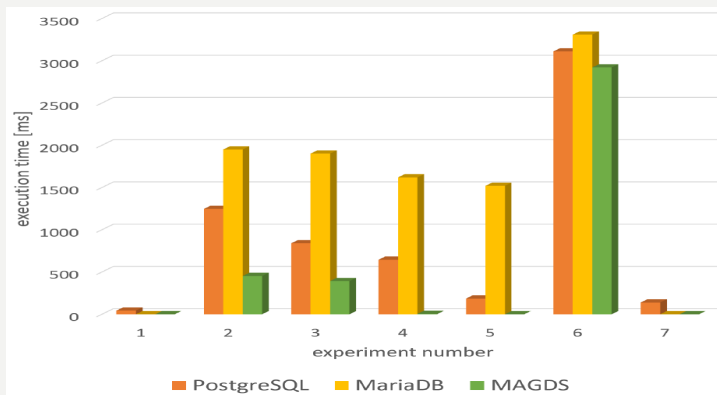
```
select max(insertsize) from prb_probe;
```

Experiment 6

```
select
sum(distinct startcoordinate) / count(distinct startcoordinate)
from map_coord_feature;
```

Experiment 7

```
select count(*) from map_coord_feature;
```



Example of another RDB

This DB contains **multiple and missing values** (DB is denormalized).

Database



table: patient

id	person_id	room_id	ICD-11
1	9	1	['CA01', 'BA00']
2	10	1	['BD11', '2F7A']
3	11	3	['EA80']
4	13	2	['EA80', 'BA00']
5	12	4	['BD11', 'EA80']
6	15	4	['2F7A', 'BA00', 'SA10']
7	16	2	['SA10']
8	14	4	['BA00', 'EA80', 'SA11']

table: person

id	first_name	last_name	age
1	Nina	Musk	35
2	John	Smith	58
3	Evelyn	Musk	42
4	John	Bush	70
5	Evelyn	Ford	70
6	Evelyn	Woods	25
7	Sara	Bosch	62
8	Cate	Smith	35
9	Lucy	Allen	70
10	Cate	Bosch	62
11	Sara	Ford	25
12	David	Smith	42
13	John	Bosch	35
14	David	Musk	58
15	Sara	Hanks	42
16	Nina	Ford	70
17	Nina	Smith	42
18	Lucy	Bush	25
19	David	Allen	35
20	Raul	Hanks	42
21	Raul	Woods	24

table: room

id	type	no_beds
1	PostOp	3
2	Emergency	3
3	Ward	4
4	Ward	5

table: doctor

id	person_id	patient_id	specialization	years_of_experience
1	2	1	Surgery	25
2	1	2	Radiology	10
3	4	4	Surgery	45
4	3	5	Oncology	17
5	18	3	Patology	2
6	20		Surgery	22
7	17	7	Radiology	25
8	19	8	Surgery	10
9	21	6	Surgery	1

table: nurse

id	person_id	room_id	years_of_experience
1	7	4	10
2	5	3	1
3	8	1	25
4	6	2	2

MAGNs can manage all these cases without any problems.



Example of another RDB

This DB contains **multiple and missing values** (DB is denormalized).

Database



table: patient			
id	person_id	room_id	ICD-11
1	9	1	['CA01', 'BA00']
2	10	1	['BD11', '2F7A']
3	11	3	['EA80']
4	13	2	['EA80', 'BA00']
5	12	4	['BD11', 'EA80']
6	15	4	['2F7A', 'BA00', 'SA10']
7	16	2	['SA10']
8	14	4	['BA00', 'EA80', 'SA11']

table: person			
id	first_name	last_name	age
1	Nina	Musk	35
2	John	Smith	58
3	Evelyn	Musk	42
4	John	Bush	70
5	Evelyn	Ford	70
6	Evelyn	Woods	25
7	Sara	Bosch	62
8	Cate	Smith	35
9	Lucy	Allen	70
10	Cate	Bosch	62
11	Sara	Ford	25
12	David	Smith	42
13	John	Bosch	35
14	David	Musk	58
15	Sara	Hanks	42
16	Nina	Ford	70
17	Nina	Smith	42
18	Lucy	Bush	25
19	David	Allen	35
20	Raul	Hanks	42
21	Raul	Woods	24

table: room		
id	type	no_beds
1	PostOp	3
2	Emergency	3
3	Ward	4
4	Ward	5

table: doctor				
id	person_id	patient_id	specialization	years_of_experience
1	2	1	Surgery	25
2	1	2	Radiology	10
3	4	4	Surgery	45
4	3	5	Oncology	17
5	18	3	Patology	2
6	20		Surgery	22
7	17	7	Radiology	25
8	19	8	Surgery	10
9	21	6	Surgery	1

table: nurse			
id	person_id	room_id	years_of_experience
1	7	4	10
2	5	3	1
3	8	1	25
4	6	2	2



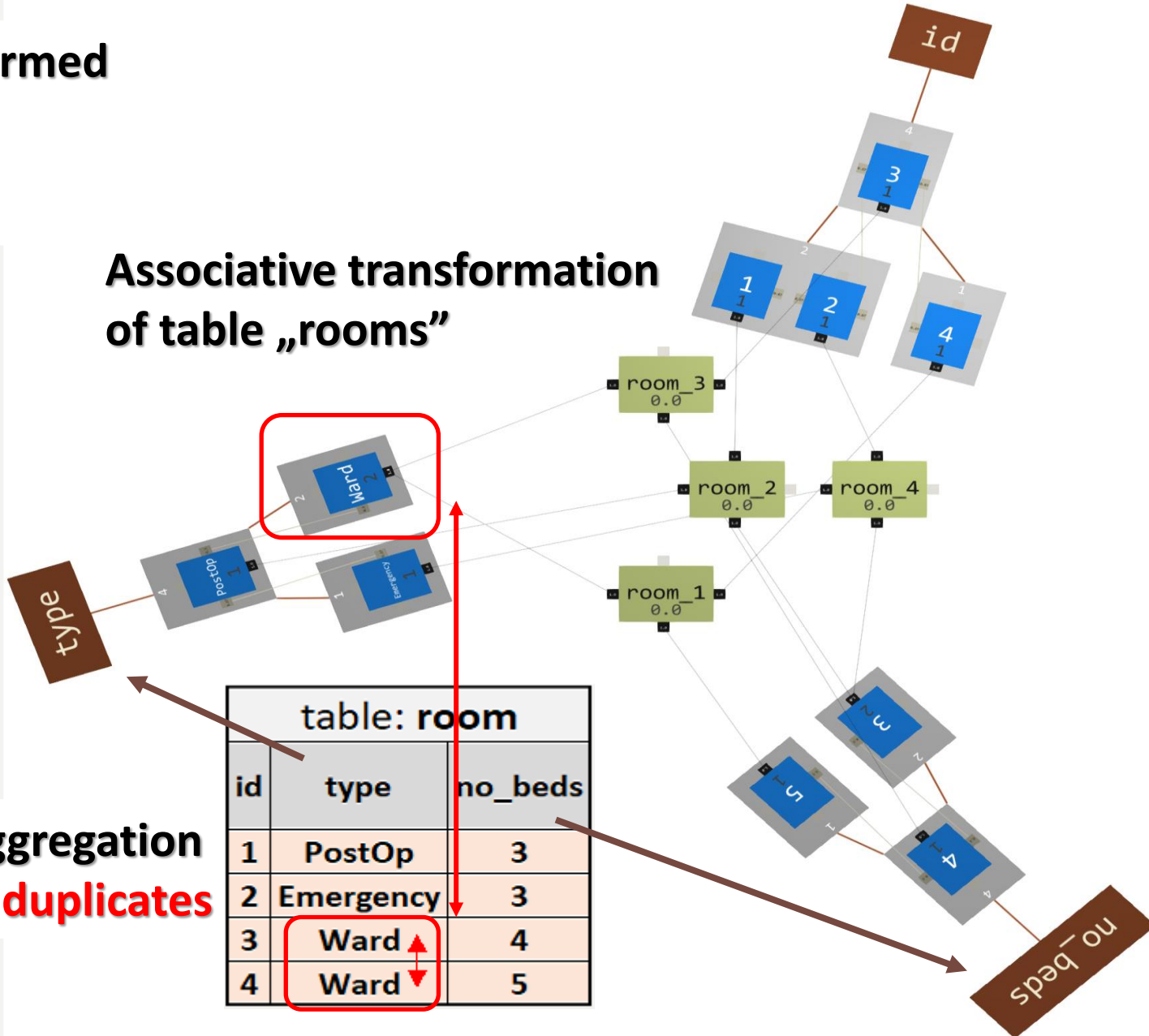
MAGNs can manage all these cases without any problems.



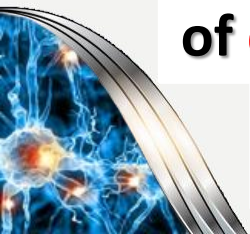
Construction Step 1

Transformed tables:
Rooms

Associative transformation of table „rooms”

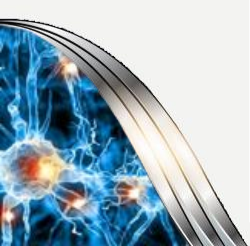
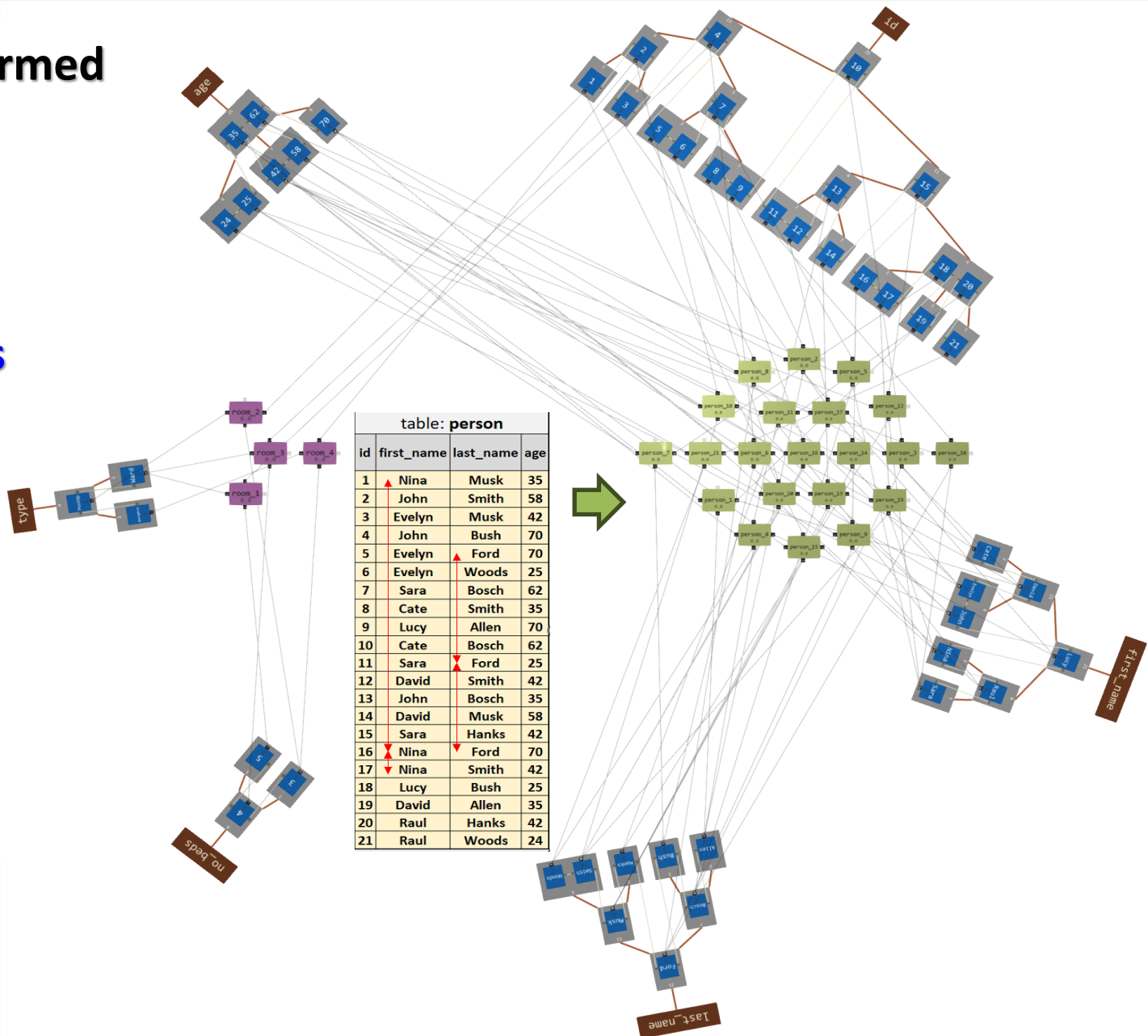


aggregation of **duplicates**



Construction Step 2

Transformed tables:
Rooms
 ↓
Persons



Construction Step 3

Transformed tables:

Rooms

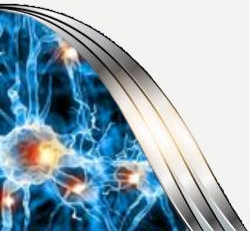
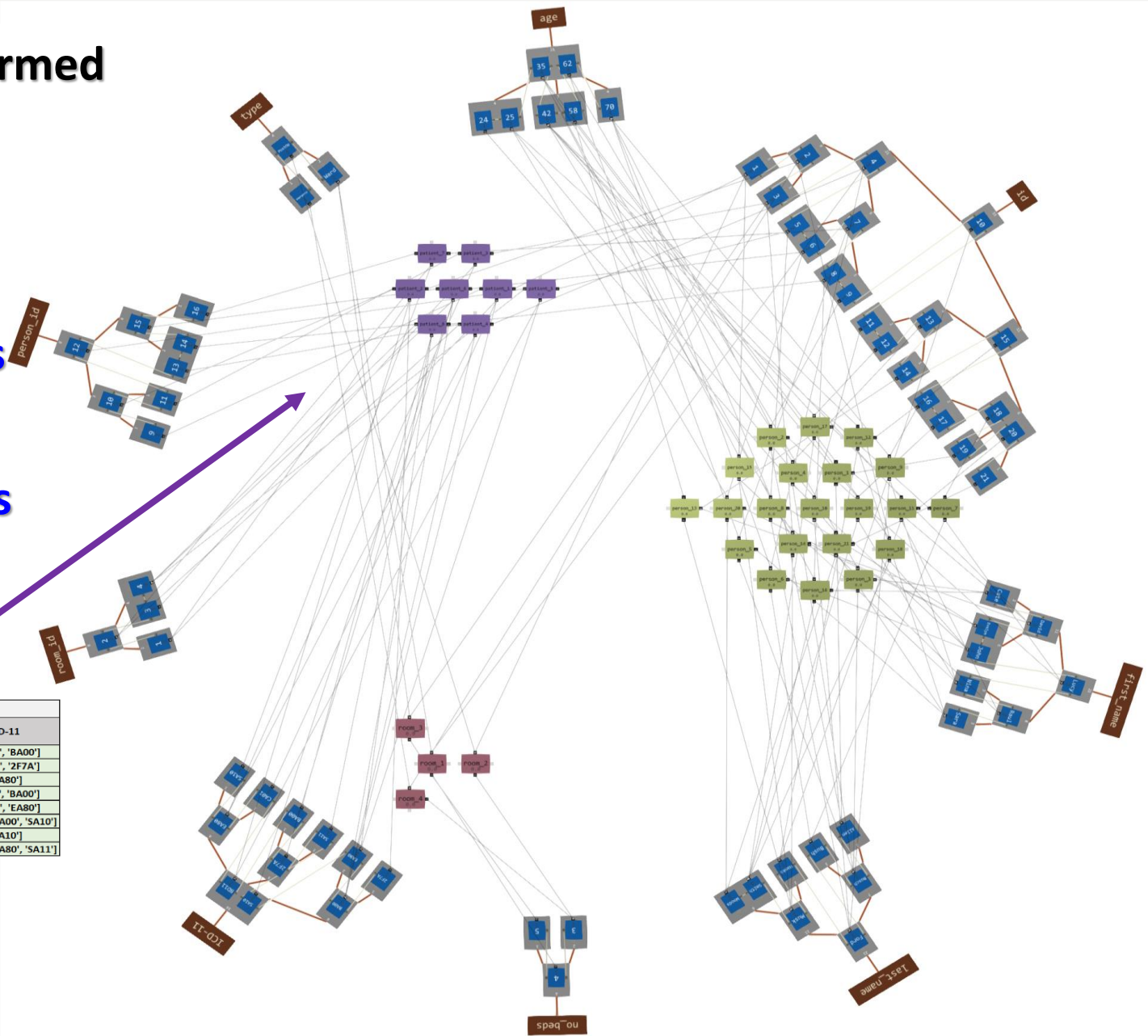


Persons



Patients

table: patient			
id	person_id	room_id	ICD-11
1	9	1	['CA01', 'BA00']
2	10	1	['BD11', '2F7A']
3	11	3	['EA80']
4	13	2	['EA80', 'BA00']
5	12	4	['BD11', 'EA80']
6	15	4	['2F7A', 'BA00', 'SA10']
7	16	2	['SA10']
8	14	4	['BA00', 'EA80', 'SA11']



Construction Step 4

Transformed tables:

Rooms



Persons

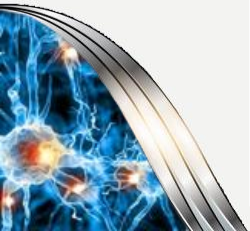
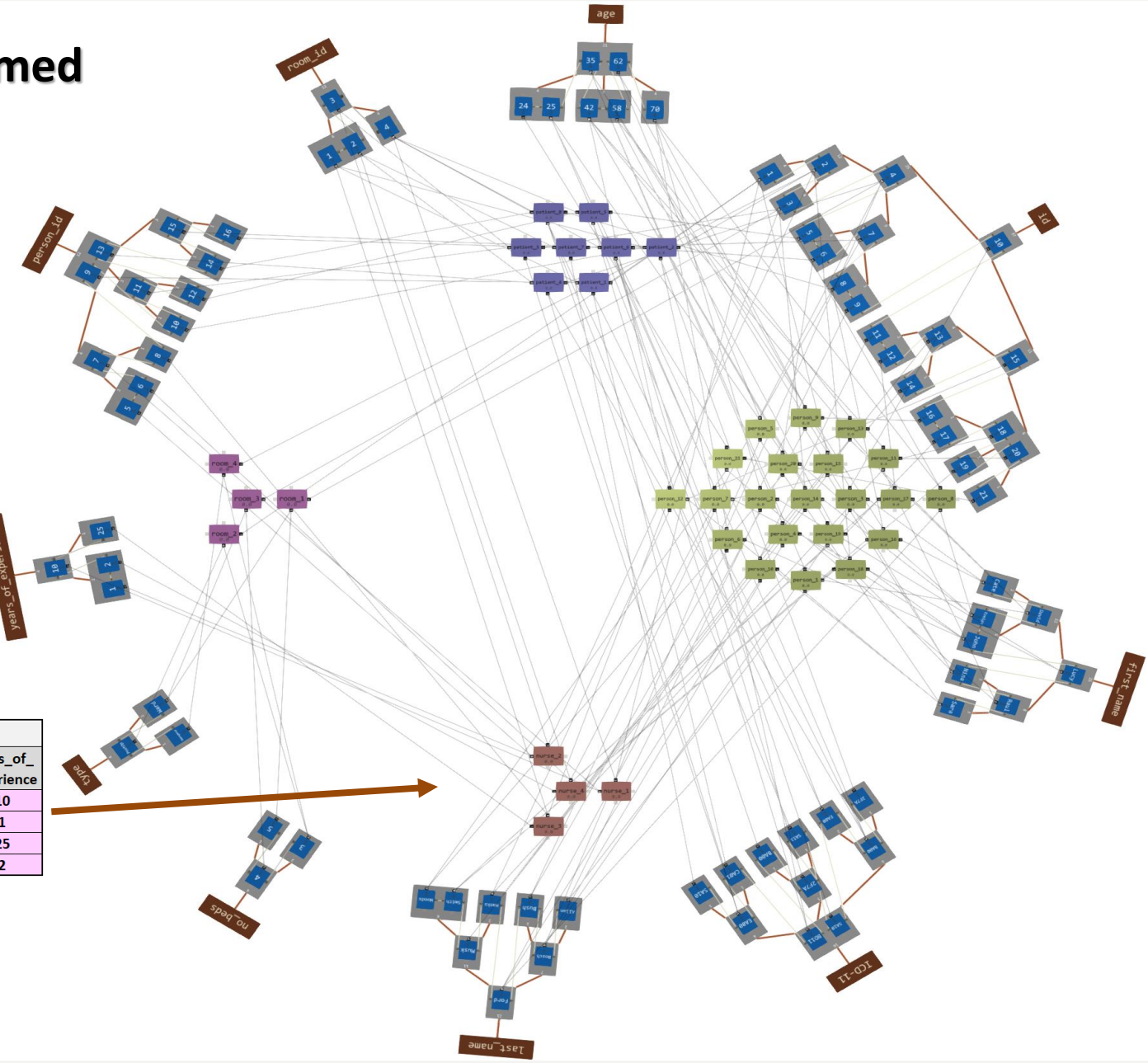


Patients



Nurses

table: nurse			
id	person_id	room_id	years_of_experience
1	7	4	10
2	5	3	1
3	8	1	25
4	6	2	2



Construction Step 5

Transformed tables:

Rooms



Persons



Patients



Nurses



Doctors

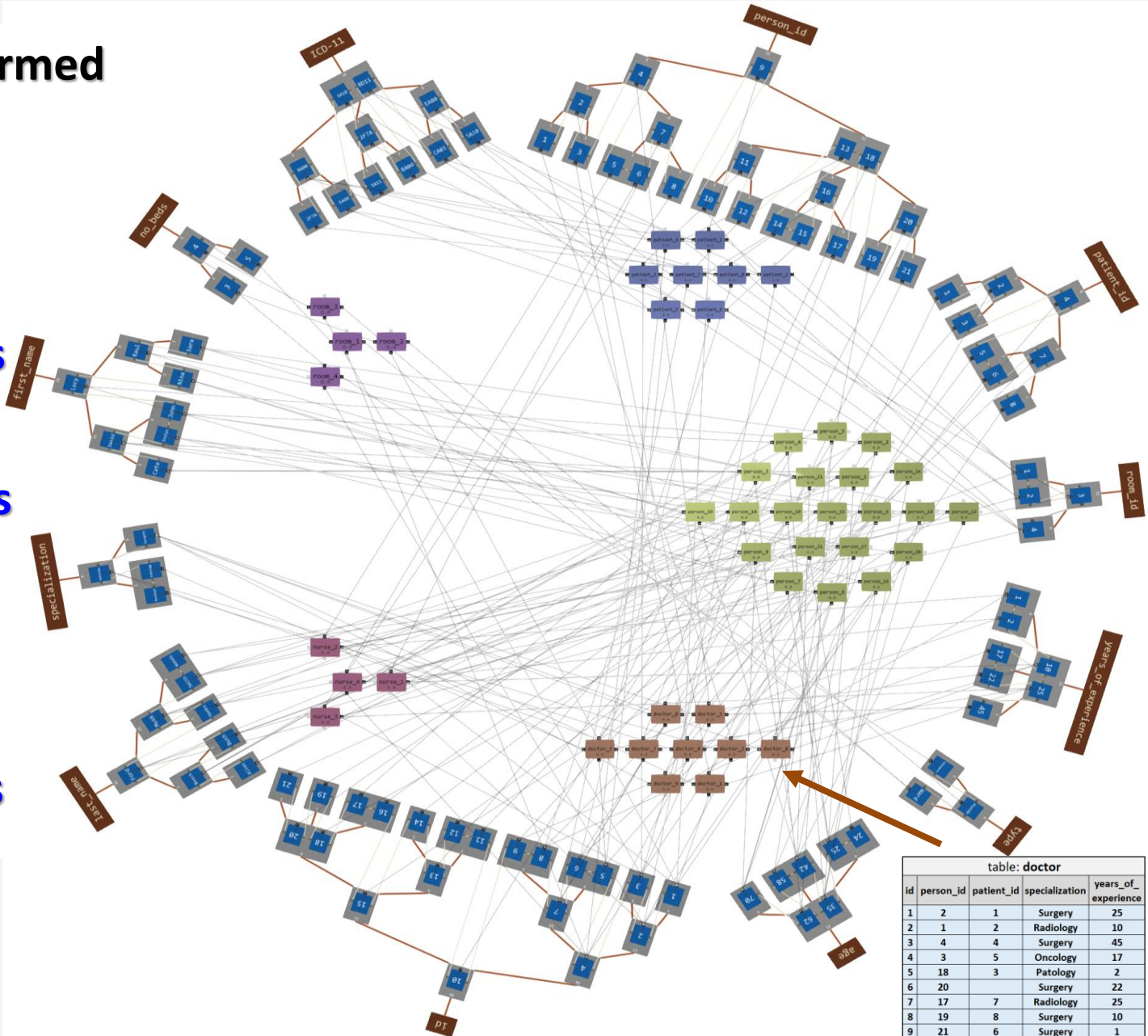
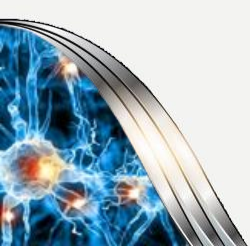
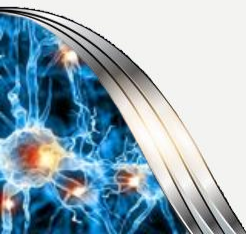
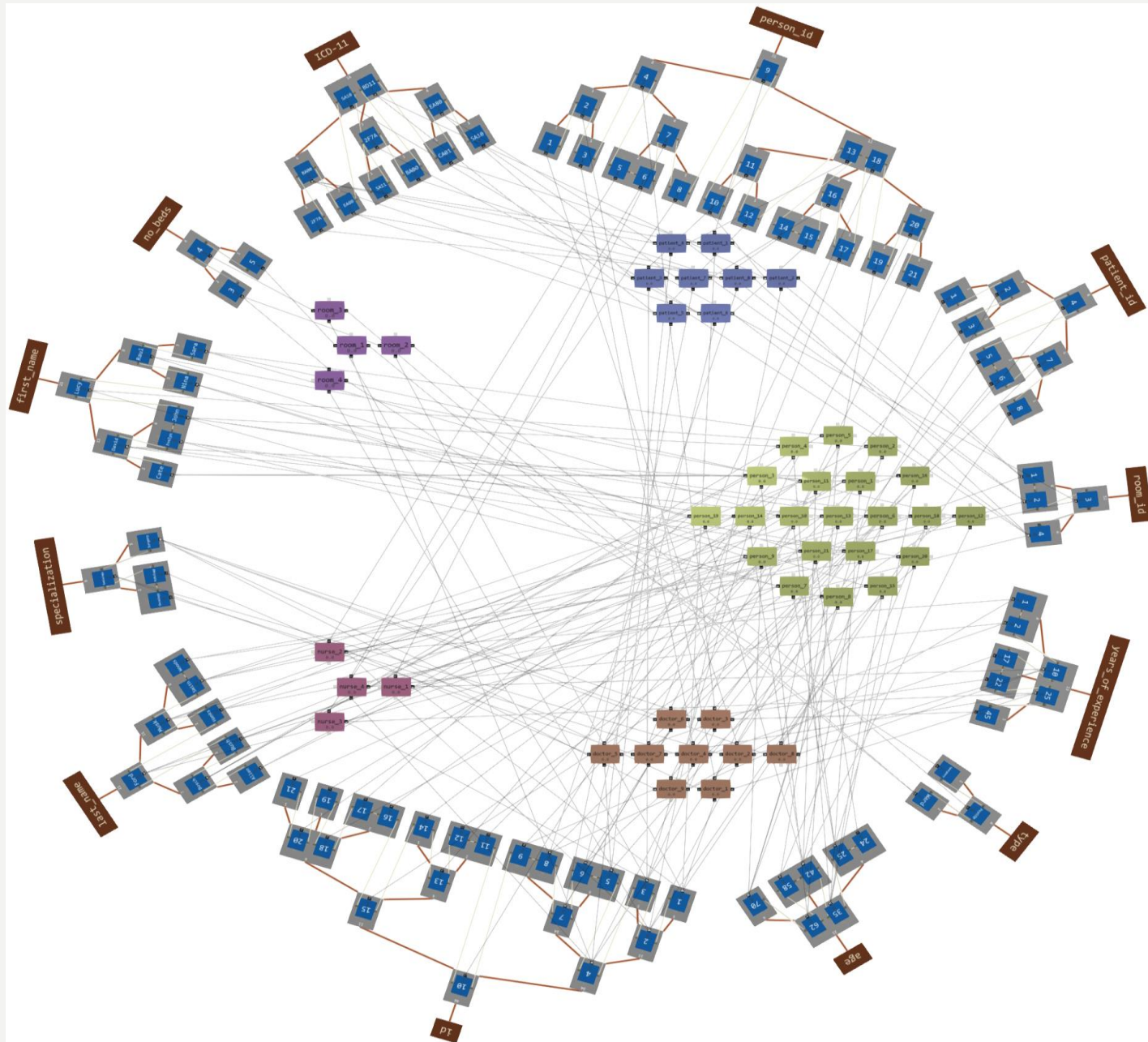


table: doctor

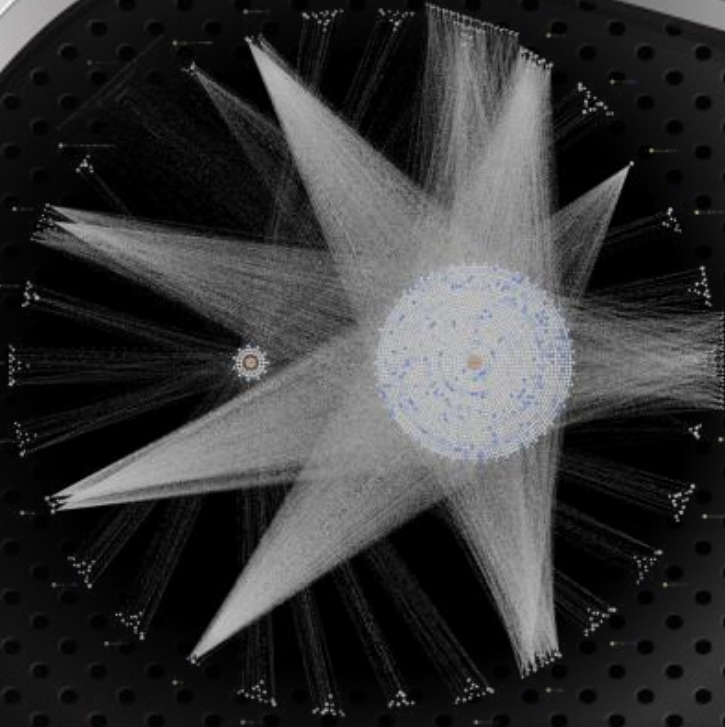
id	person_id	patient_id	specialization	years_of_experience
1	2	1	Surgery	25
2	1	2	Radiology	10
3	4	4	Surgery	45
4	3	5	Oncology	17
5	18	3	Patology	2
6	20	3	Surgery	22
7	17	7	Radiology	25
8	19	8	Surgery	10
9	21	6	Surgery	1



MAGN Constructed and Weights Calculated



ECML PKDD 2023



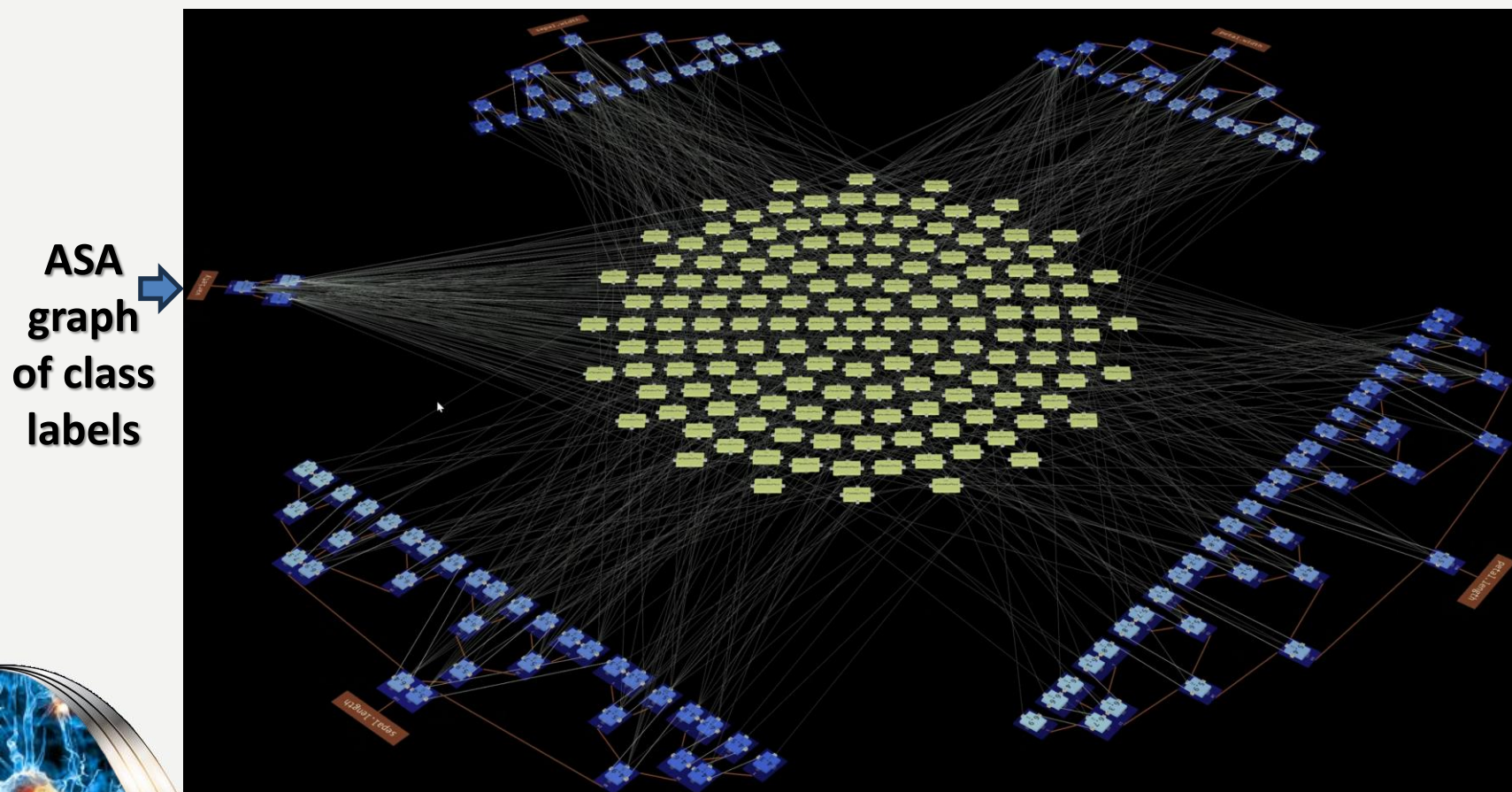
Multi-Associative Graph Networks for Classification and Regression

Construction and Training of
Multi-Associative Graph Networks



MAGN Classification and Regression

MAGNs can be successfully used for classification and regression tasks defined by tables of training examples or databases, where **we do not need to specify which attribute contains labels** (classes, predicted values) before constructing MAGNs. We can do it at any time later!

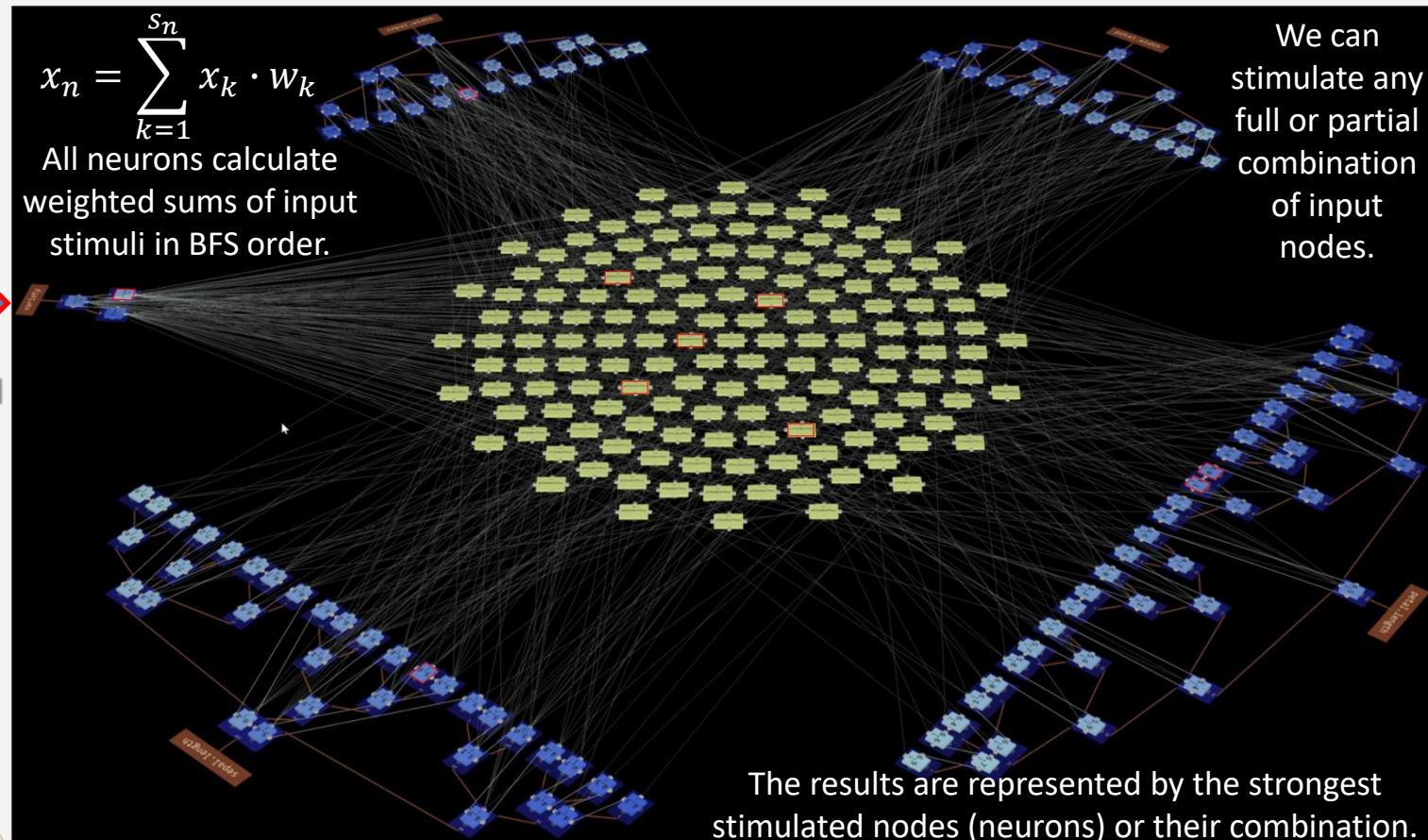


The MAGN constructed for IRIS training data.



Constructed MAGN Exploitation

MAGNs can be exploited in many different ways. We can **freely choose input and output (target) attributes**, stimulate any combination of input nodes, propagate stimulation through this network according to the calculated weights in the BFS order, and read out the mostly stimulated output nodes.



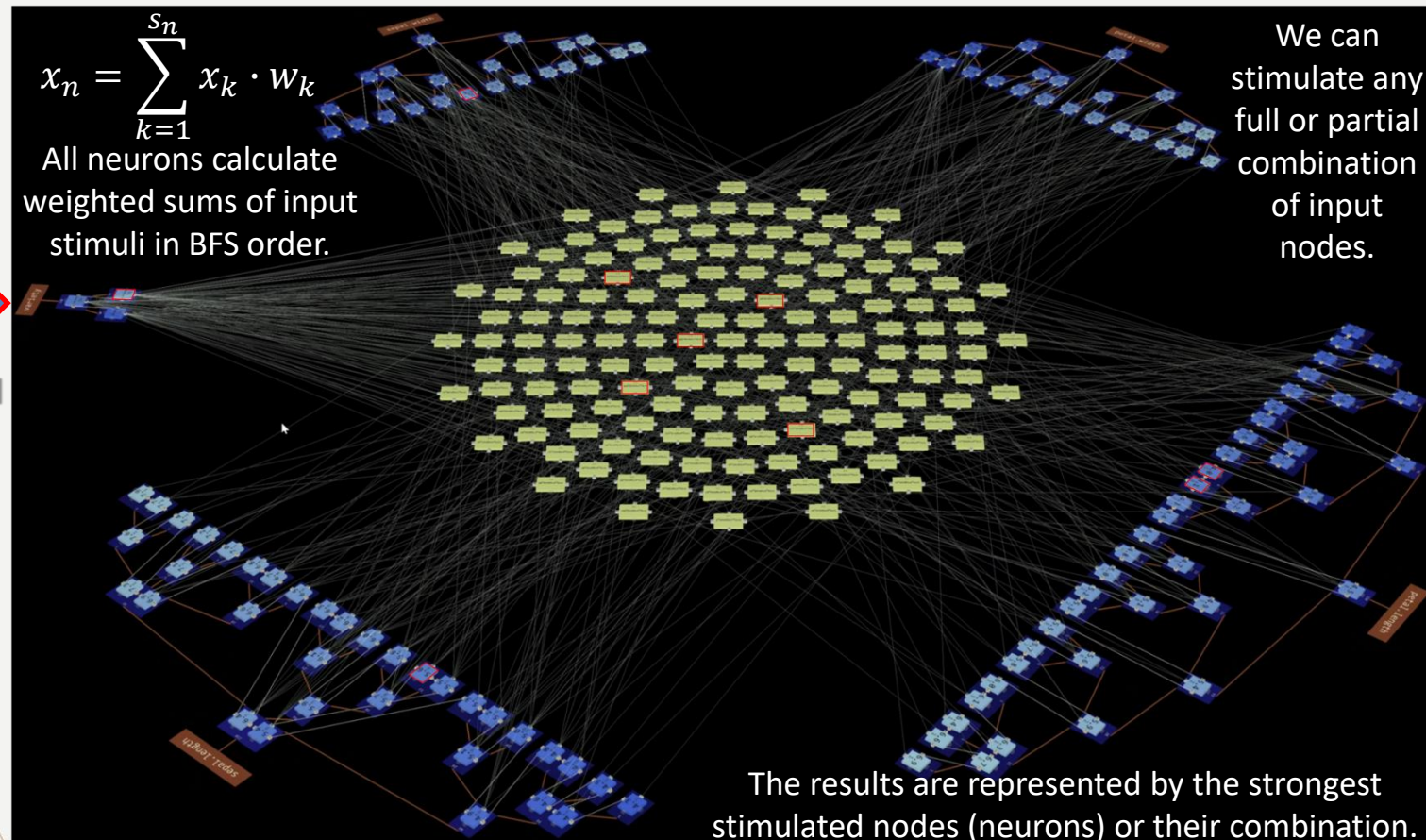
It points **the strongest associated nodes to the input context.**



Sparse MAGN Connections

Sparse MAGN connections represent **essential relationships** between values and objects represented by this graph structure. The **weights** of these connections reproduce the **importance of these relationships**.

Sparse connections resemble **hard attention**, while **weights** **soft attention**.



It points **the strongest associated nodes to the input context**.

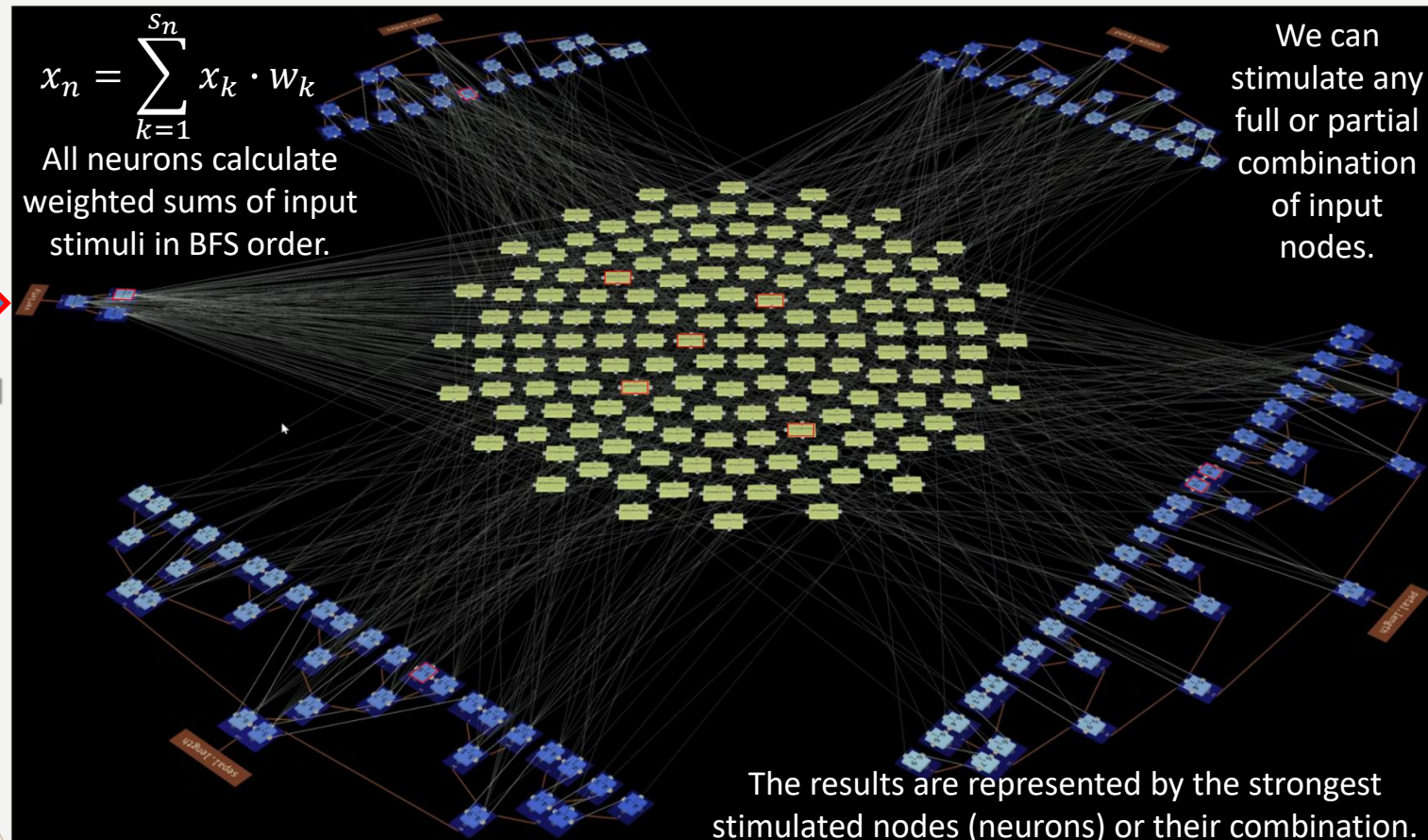



MAGN Classification & Regression

Classification results are pointed by **the strongest stimulated label nodes**.

Regression results are calculated based on **the strongest stimulated numerical nodes** of the attributes pointed as outputs (targets).

We can **change targets without retraining the network** and solve diverse tasks.



The  strongest stimulated class neuron (node) represent the answer.

It points **the strongest associated nodes to the input context**.





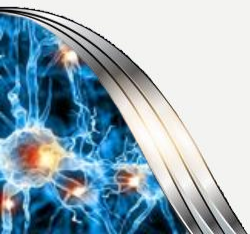
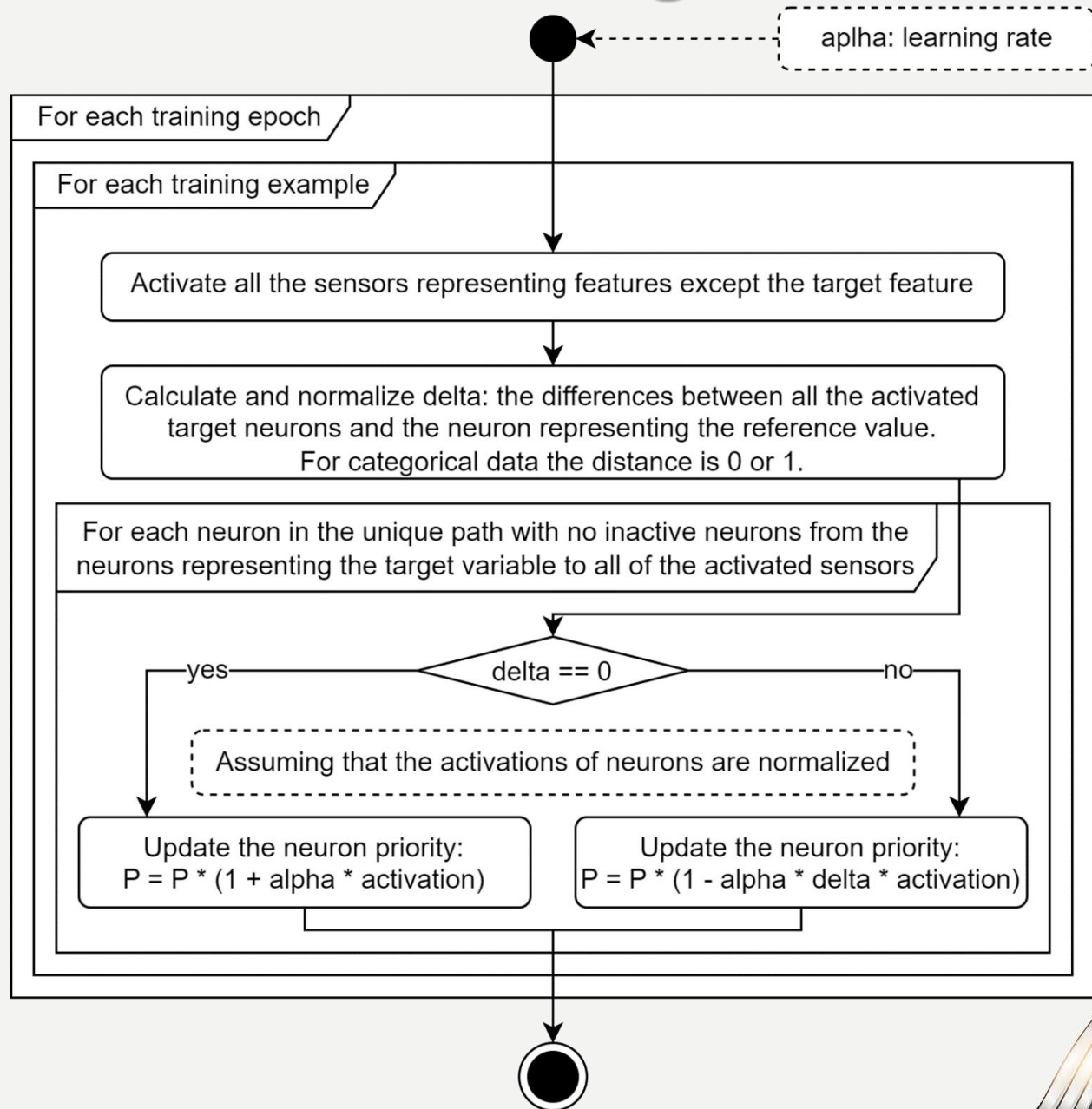
Prioritization Algorithm for data and relationship soft-attention

Construction and Training of
Multi-Associative Graph Networks

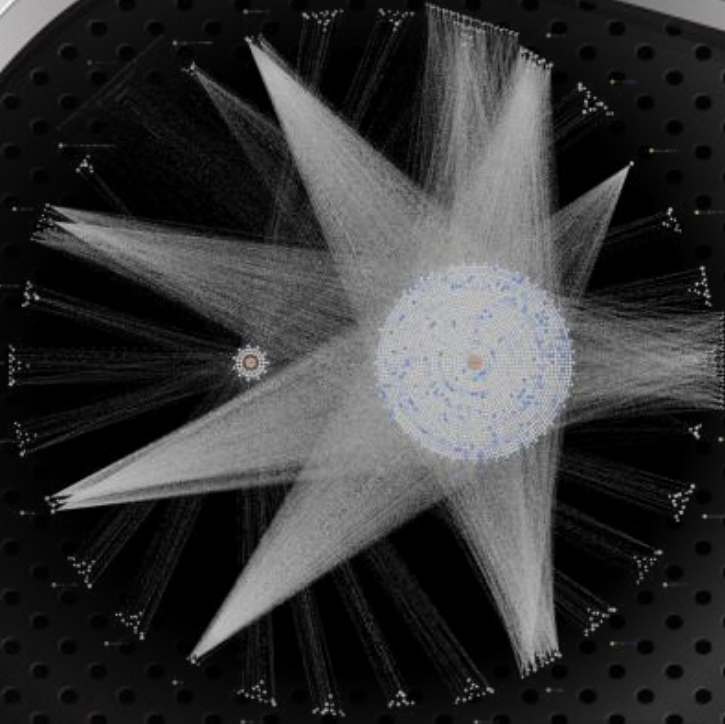


MAGN Prioritization Algorithm

It allows us to add **attention** to data and relationships, **strengthening** or **weakening** impact of the **nodes** of this structure to achieve still better results of regression and classification.



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Multi-Associative Graph Networks

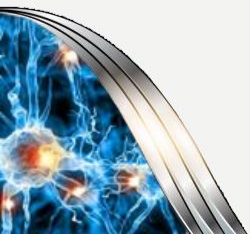
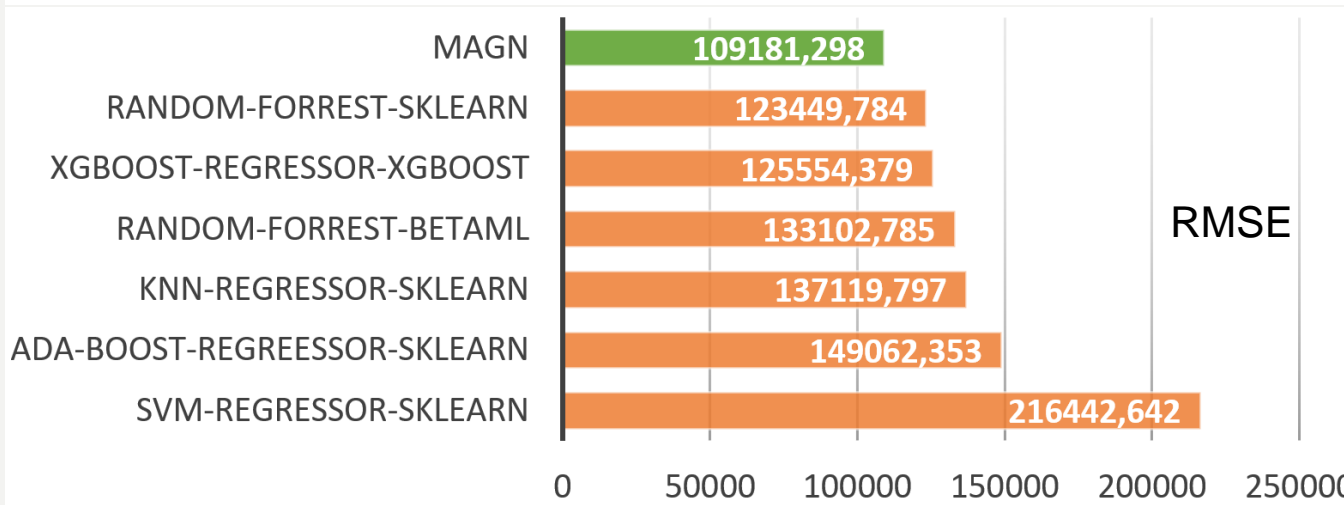
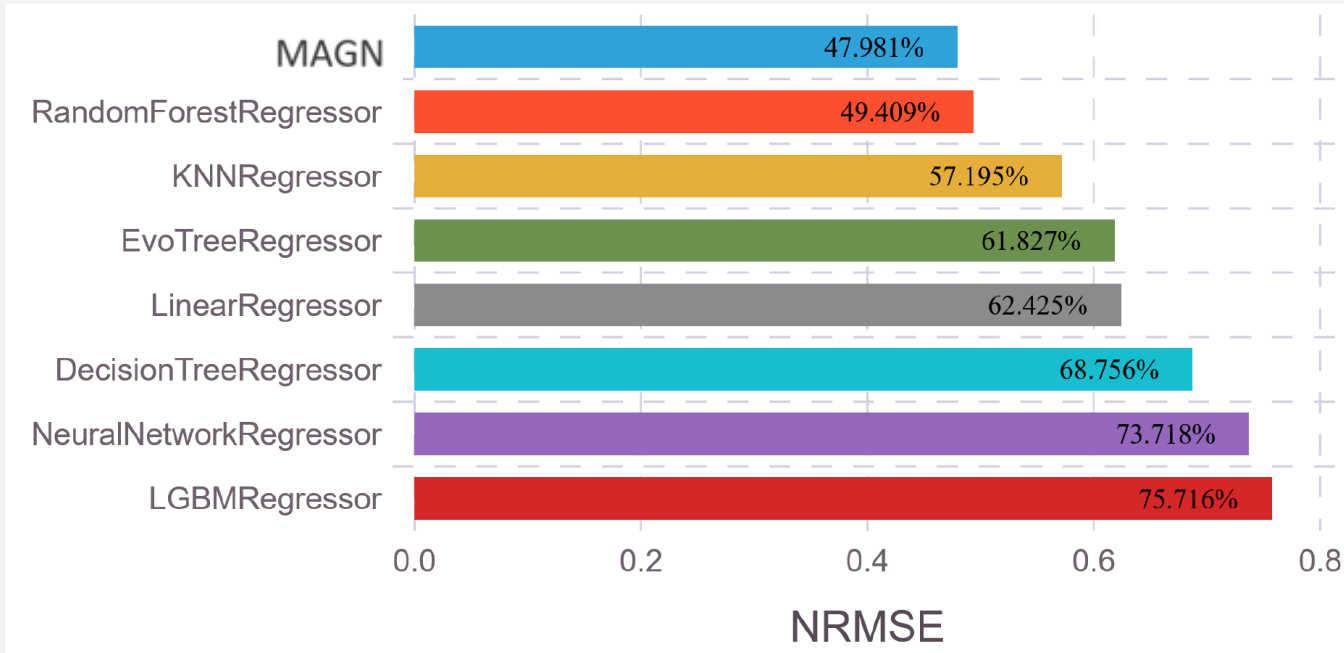
Experimental Results
and Comparisons
to SOTA Methods

Construction and Training of
Multi-Associative Graph Networks



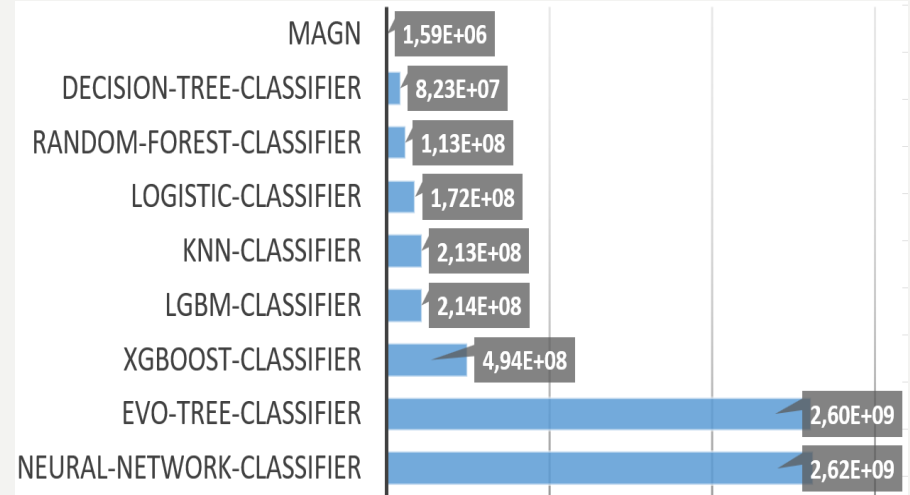
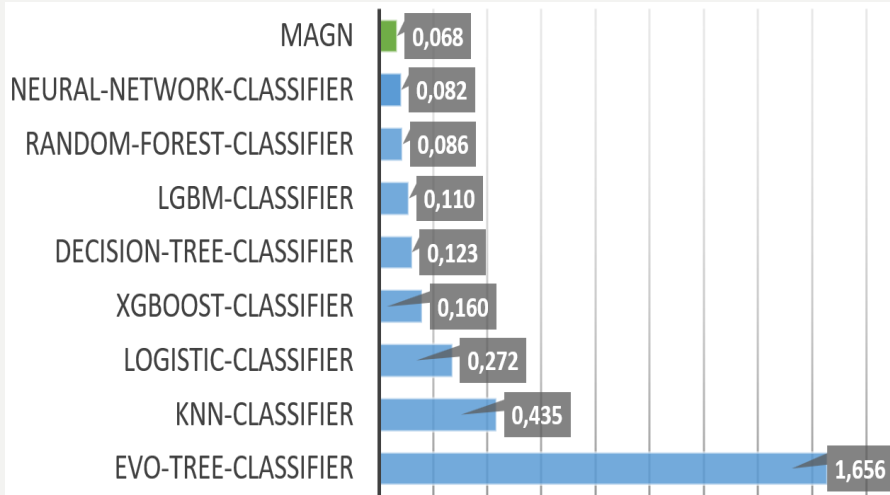
Experiments & Comparisons

Comparisons of the results collected for regression 18 training datasets:



Experiments & Comparisons

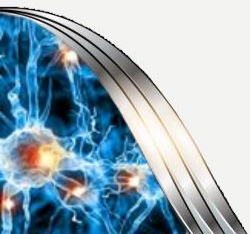
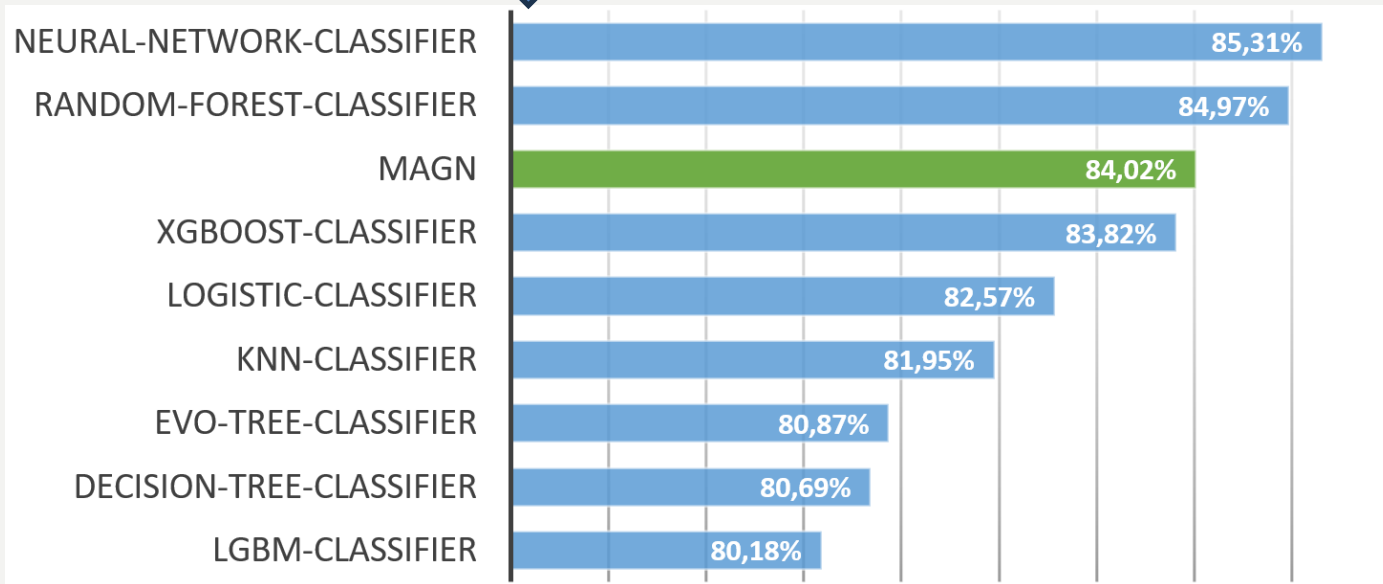
Comparisons of the results collected for classification 73 training datasets:



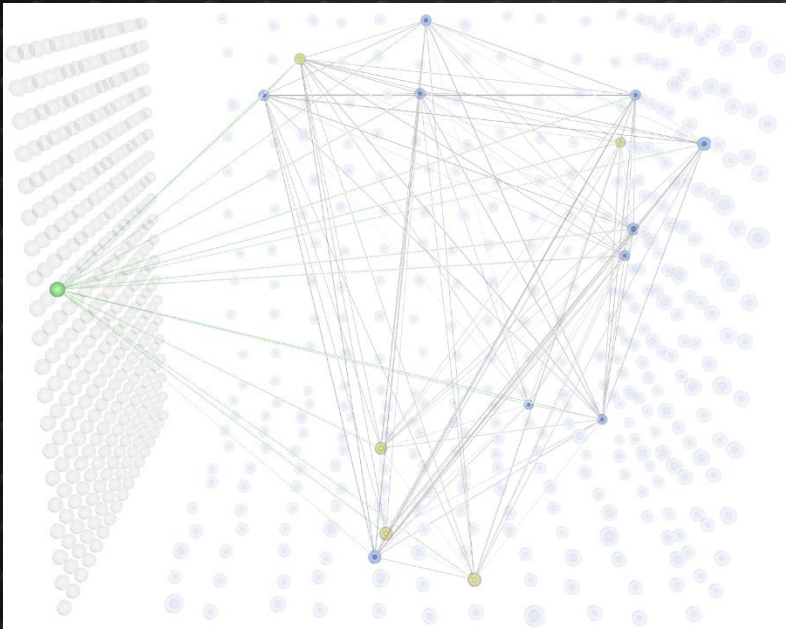
Execution Time ↑

↓ **Mean Accuracy**

↑ **Allocated Memory**



Commercial Deployment & Conclusions



Construction and Training of
Multi-Associative Graph Networks



MAGN implementation and source code

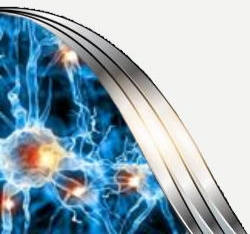


The MAGN source code is available at
<https://github.com/danbulnet/witchnet>

The source code can be downloaded and compiled on multiple platforms. There are no specific minimal hardware requirements; however, since this is an in-memory model, the amount of RAM should scale with the amount of data being modeled. The code was tested on popular 64-bit operating systems, such as Windows 11, MacOS 13, and Linux Endeavour OS 2023.



Benchmark source code is available at
<https://github.com/danbulnet/WitchnetBenchmarks.jl>

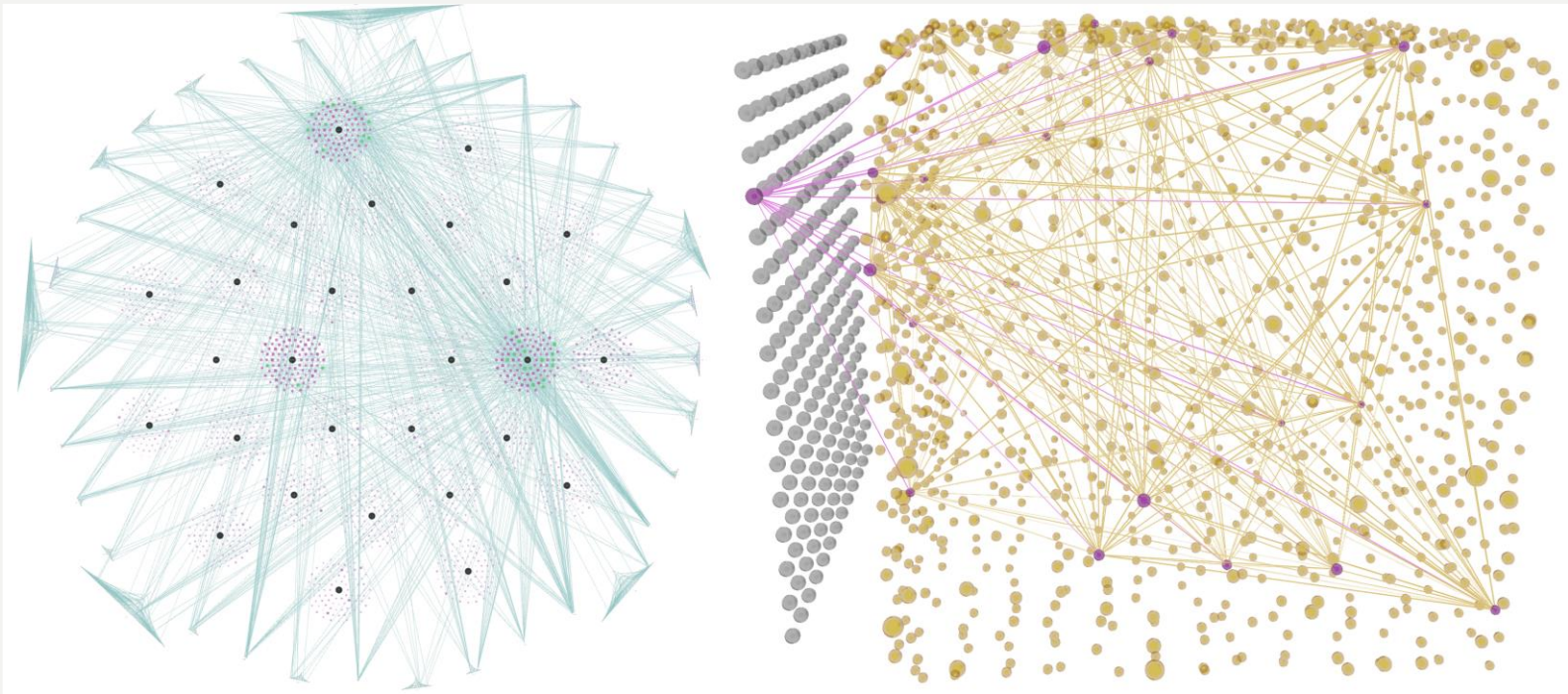


Commercial Deployment

MAGNs are under commercial deployment in cooperation with:



grape up[®]



<https://grapeup.com/blog/associative-knowledge-graphs/>





Conclusions and Final Remarks

- ✓ **MAGNs** are fully **scalable** and **explainable** models that can be used for **classification** or **regression** of vectorized data stored in databases.
- ✓ They can be very **quickly** constructed and **fast** evaluate and answer.
- ✓ Training data can be **updated** at any time **without model „retraining“**.
- ✓ They can be **constructed without specifying „labels“** that can be chosen later, i.e., every attribute can be chosen as target without „retraining“.
- ✓ They can be used as associative knowledge graphs to store information about associated objects of one or many databases **parsimoniously**.
- ✓ They can be used for **searching** for various data and relationships in any given context. The results are **legible** and **easy interpretable**.
- ✓ They can **cluster, classify, predict, recommend, group, recognize, find associations...** of any vectorized data stored in RDBs used in **MAGNs**.

Welcome to the poster for further discussions

Construction and Training of Multi-Associative Graph Networks

AGH University of Krakow, Poland | Session S4-A71 | GRAPHS 2 | 20.09.2023 | 16:30-18:30 | ECML PKDD

OHIO STATE UNIVERSITY | University of Information Technology and Management in Rzeszow, Poland

Adrian Horzyk | Daniel Bulanda | Janusz A. Starzyk

Brain inspired

Problem Definition

How to operate on database objects and their relations in brain-like ways using associations for classification and knowledge representation?

Methodology

Associate data and objects of all tables of all DBs by:
- Aggregating duplicates and representing them the same nodes.
- Sorting data in alphanumeric or symbolic order to connect them in order.
- Connecting nodes representing similar values and related objects in the graph.

Additionally, we prioritize (adapt the soft attention) the values of some nodes according to their importance for the classification process:

ASA-graph

attribute pairs of appearance
B-tree branches
input definition connections

Results

The results collected for classification and regression benchmark training datasets prove the efficiency of MAGNs:

- From ML Classification Benchmarks for 73 datasets with less than 1000 records.
- From ML Regression Benchmark Comparisons for 18 datasets.

Mean Accuracy, Normalized Root Mean Squared Error (NRMSE), Mean Execution Time of the inference phase in seconds, Execution Time, Mean Allocated Memory during the entire benchmark (training and inference phases) in bytes.

Associative Transformation

Such results were possible because MAGN structures are constructed to reproduce specific relationships of every dataset or database. The sparse connections created in the construction process reproduce real relationships supporting predictions.

Commercial Deployment

grape up®

Conclusions

1. Sparse associative connections work like hard attention allowing the MAGNs to focus only on essential relationships.
2. The weights reproduce the strengths of these relationships, defined by the frequency of occurrences of values and objects.
3. This strategy does not require a long-lasting training process.

References

Adrian Horzyk, Daniel Bulanda, and Janusz A. Starzyk, Construction and Training of Multi-Associative Graph Networks, Proc. of 2023 European Conference on Machine Learning (ECML PKDD 2023), Part III, LNCS 14171, Chapter 17, Springer, 2023.
A. Horzyk, D. Bulanda, J. A. Starzyk, ASA-graphs for Efficient Data Representation and Processing, International Journal of Applied Mathematics and Computer Science (AMCS), Vol. 30, No. 4, 2020, pp. 717 - 731, DOI: 10.34768/amcs-2020-0053



Research papers:





Construction and Training of Multi-Associative Graph Networks



[Adrian Horzyk](#)



Daniel Bulanda



[Janusz A. Starzyk](#)



AGH University of Krakow - University of Information Technology and Management in Rzeszow - Ohio University in Athens



Torino

ECML PKDD 2023

September 18 - 22 2023



Bibliography and Associated Works

- ✓ **A. Horzyk, J.A., Starzyk, J. Graham, Integration of semantic and episodic memories, IEEE transactions on neural networks and learning systems 28(12), 2017, 3084–3095.**
- ✓ **Basawaraj, J.A. Starzyk, A. Horzyk, Episodic memory in minicolumn associative knowledge graphs. IEEE transactions on neural networks and learning systems 30(11), 2019, 3505–3516.**
- ✓ **A. Horzyk, Associative graph data structures with an efficient access via AVB+trees. In: 2018 11th International Conference on Human System Interaction (HSI), IEEE, 2018, 169–175.**
- ✓ **A. Horzyk, Associative representation and processing of databases using DASNG and AVB+trees for efficient data access. In: Knowledge Discovery, Knowledge Engineering and Knowledge Management: 9th International Joint Conference, IC3K, 2017, Funchal, Madeira, Portugal, November 1-3, 2017, Revised Selected Papers 9, Springer, 2019, 242–267.**
- ✓ **A. Horzyk, D. Bulanda, J.A. Starzyk, ASA-graphs for efficient data representation and processing. International Journal of Applied Mathematics and Computer Science 30(4), 2020, 717–731.**
- ✓ <https://grapeup.com/blog/associative-knowledge-graphs/>
- ✓ <https://github.com/PrzemyslawStok/Structural-Properties-of-Associative-Knowledge-Graphs>